

Reconnection & ion heating

in low- β hybrid-kinetic plasma turbulence

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Séminaire Lagrange

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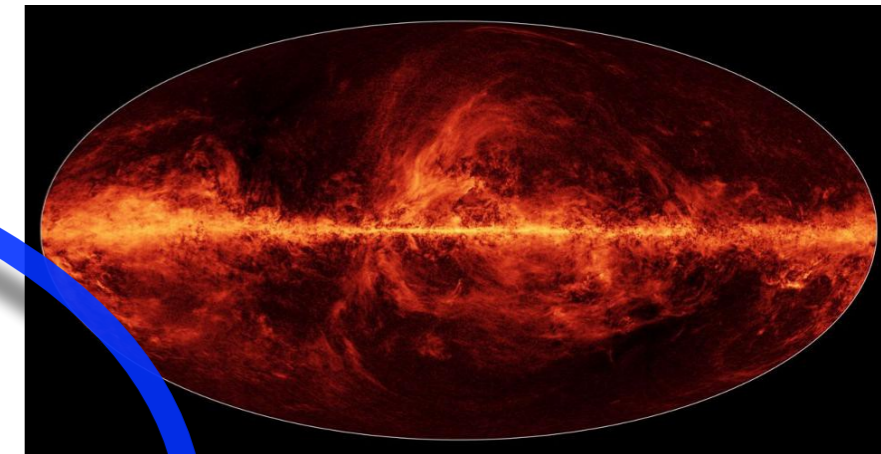
Outline

- Turbulence & heating in astrophysical and space plasmas
 - ☞ Why do we care about turbulence in “collisionless” plasmas?
 - ☞ The solar wind & space missions (*or, “where we can really learn something about plasma turbulence”*)
 - ☞ What (we think) we know about plasma turbulence and turbulent heating
 - ☞ The NASA Parker Solar Probe mission
- The hybrid-PIC code `PEGASUS` & simulation setup
- Magnetic reconnection & spectral features of quasi-steady state turbulence
- Ion heating

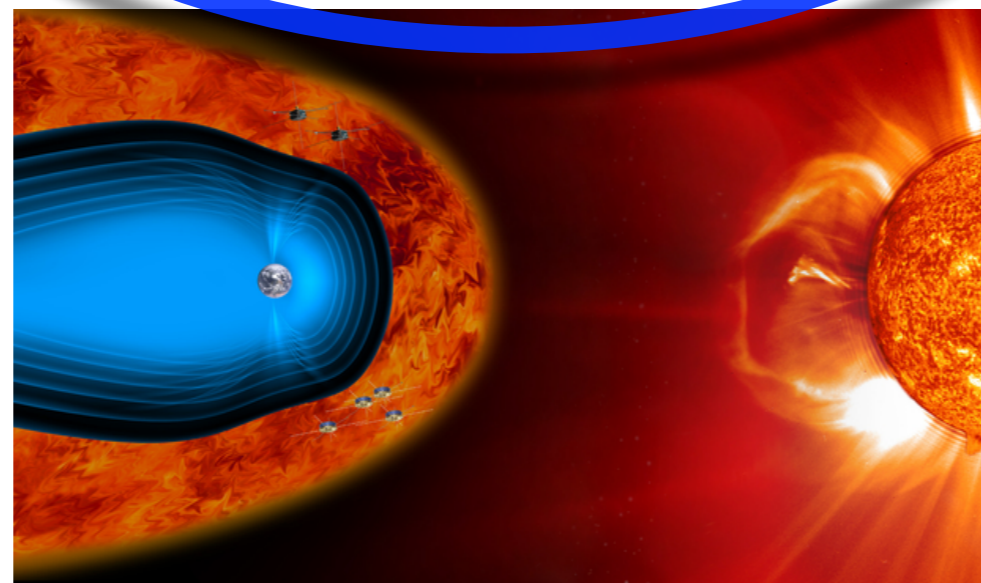
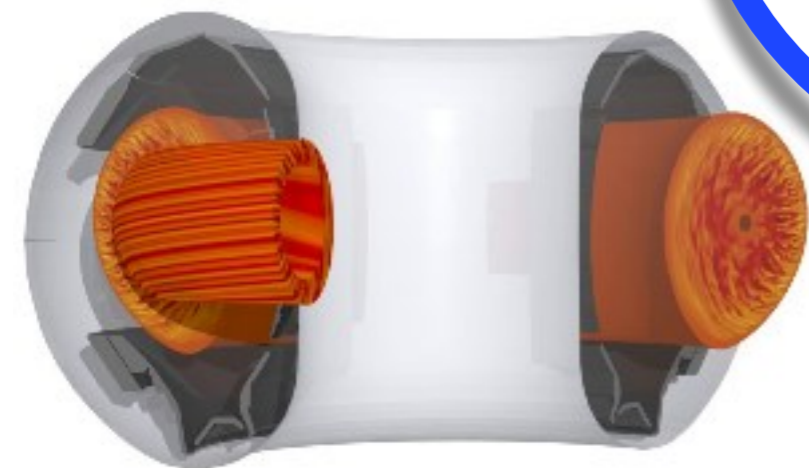
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Turbulence in “collisionless” plasmas



**Plasma
Turbulence**



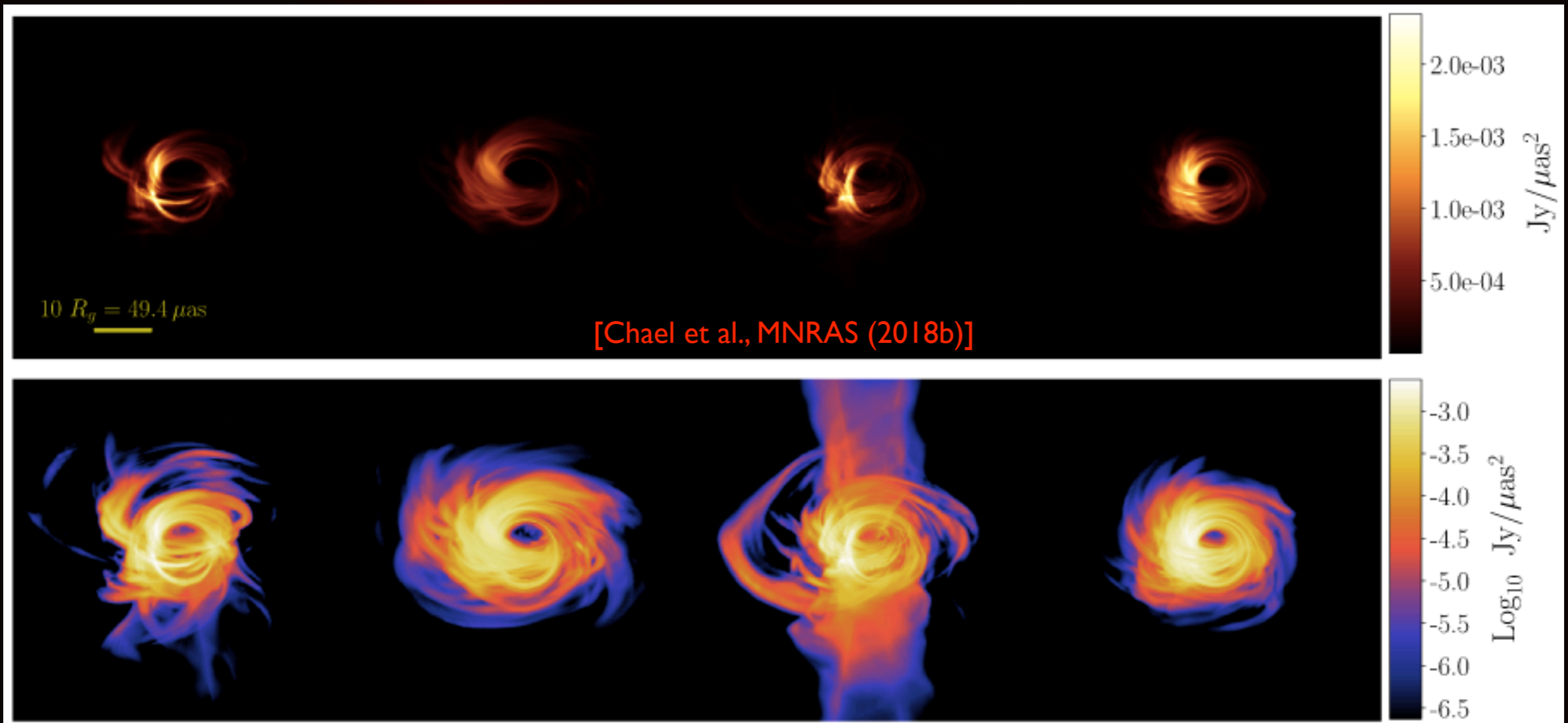
Turbulence in “collisionless” plasmas

[credit: Event Horizon Telescope Collaboration]



Turbulence in “collisionless” plasmas

[credit: Event Horizon Telescope Collaboration]

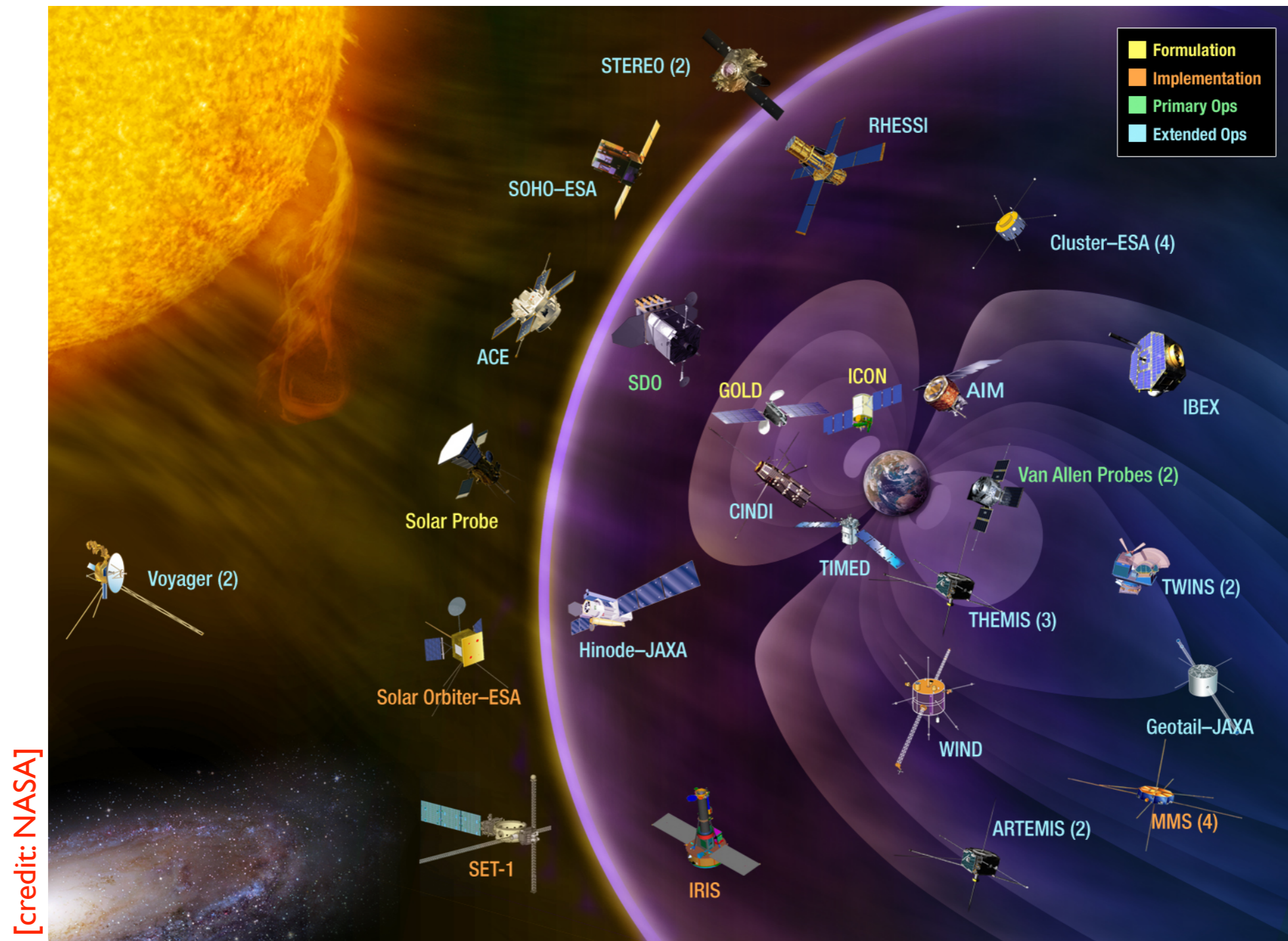


***Turbulent heating + energy partition among species
→ determine several emission features!***

Outline

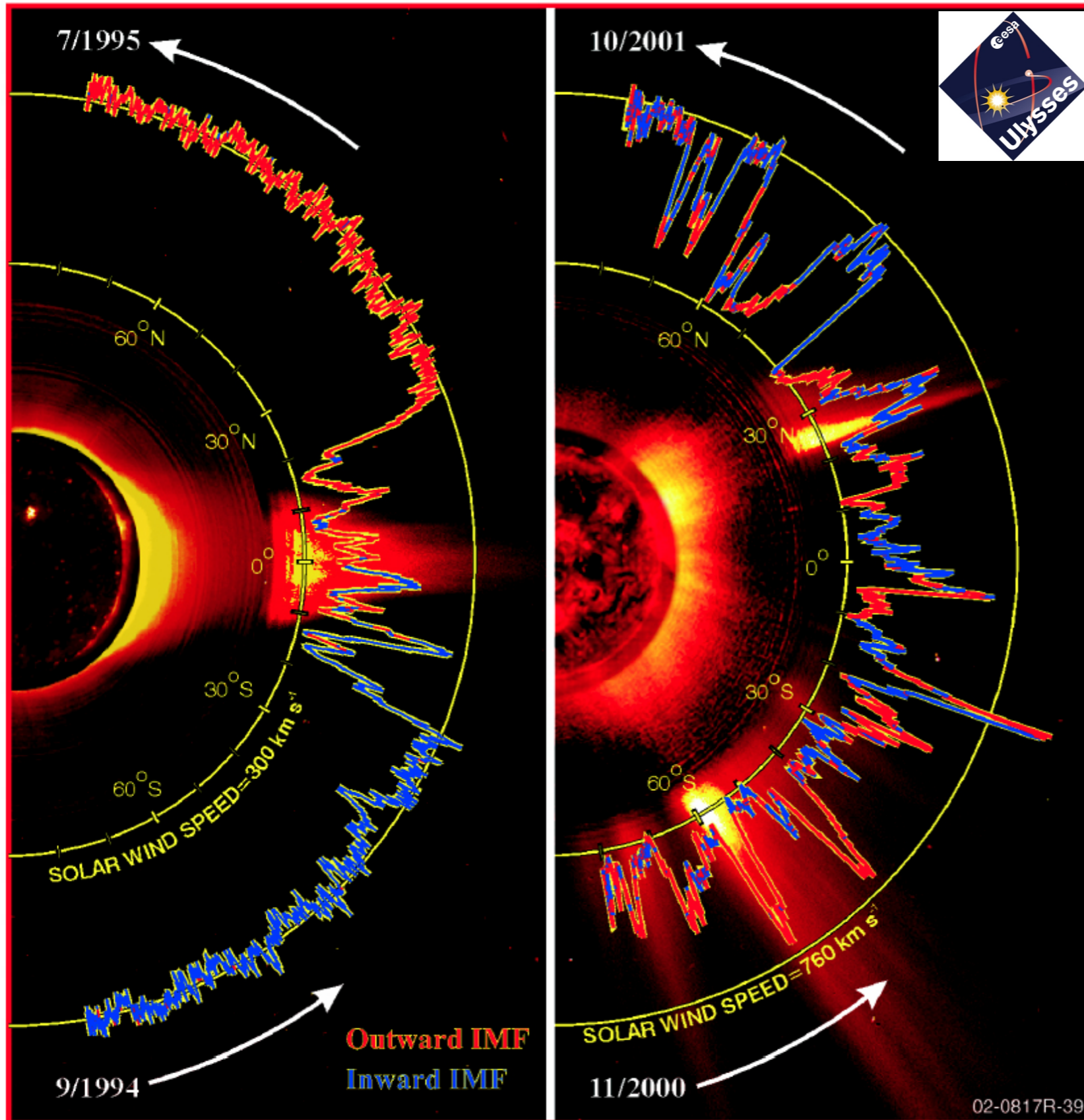
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Near-Earth's environment & Solar Wind



Increasingly accurate in situ measurements have become available

The Solar Wind (SW)

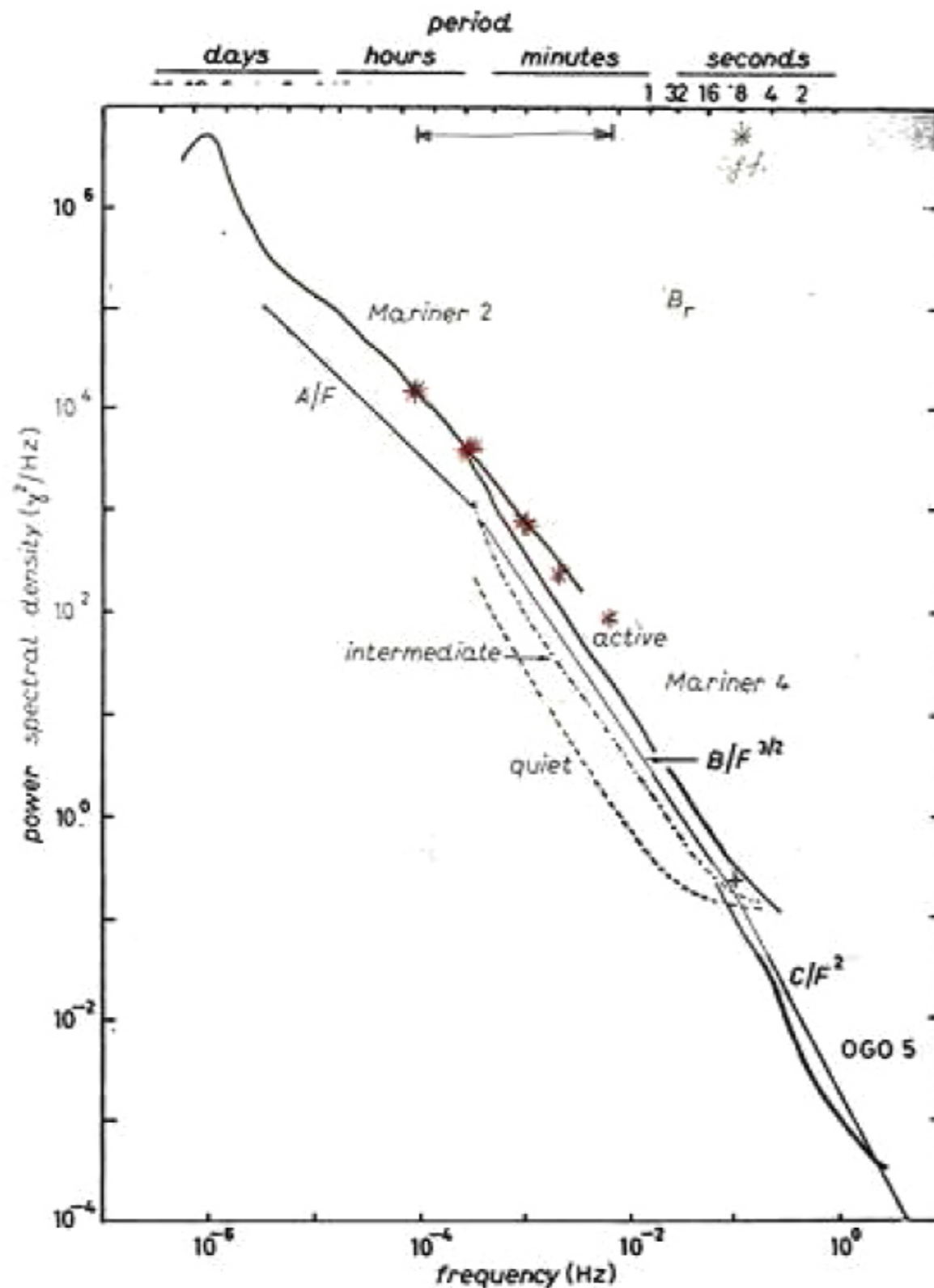
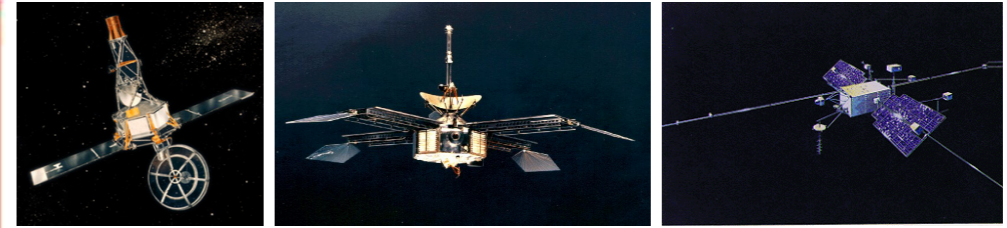


- Continuous flow of (globally neutral) charged particles from our star: Solar Wind (SW)
- SW is mostly found in a **turbulent state**
- Time and space variability due to solar cycles and turbulent evolution: quite large parameter space
- SW plasma is “**collisionless**”

***kinetic treatment
is eventually
necessary!***

[credit: ESA]

Early observations of SW turbulence



Early observations of **magnetic fluctuations power spectrum** as function of frequency from *Mariner 2*, *Mariner 4* and *OGO 5*:

- Injection range: $\sim f^{-1}$
- “intermediate” range: $\sim f^{-1.5}$
- “final” range: $\sim f^{-2}$

NOTE:

frequencies (f) in the spacecraft frame can be turned into wavenumbers (k) via **Taylor hypothesis**: $2\pi f \approx \mathbf{k} \cdot \mathbf{V}_{\text{sw}}$

[credit: Bruno & Carbone, LRP (2005); see Russel (1972) therein]

Early observations of SW turbulence

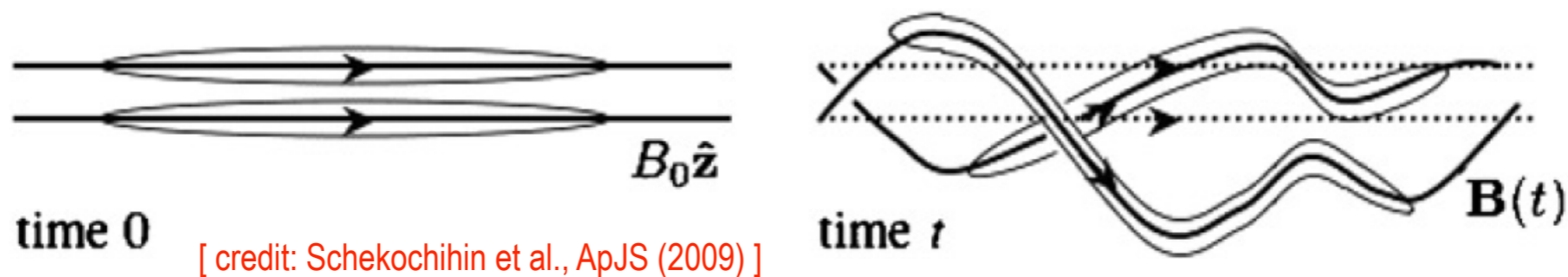
MHD turbulence in a nutshell

[neutral fluid case: $\sim k^{-5/3}$ (Kolmogorov: *isotropic hydrodynamic turbulence*)]

- $\sim k^{-3/2}$ (Iroshnikov & Kraichnan: *isotropic MHD turbulence*)
- $\sim k_{\perp}^{-5/3}$ & $\sim k_{\parallel}^{-2}$ (parallel and perpendicular with respect to \mathbf{B});

anisotropy from “*critical balance*”: $k_{\parallel} \sim k_{\perp}^{2/3}$

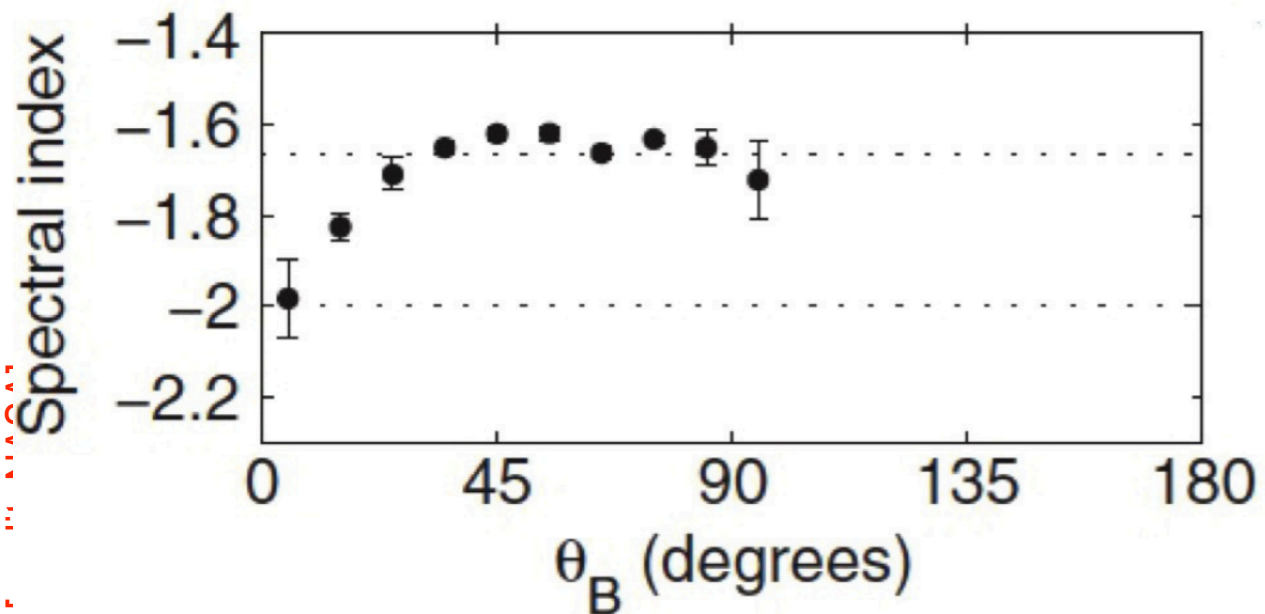
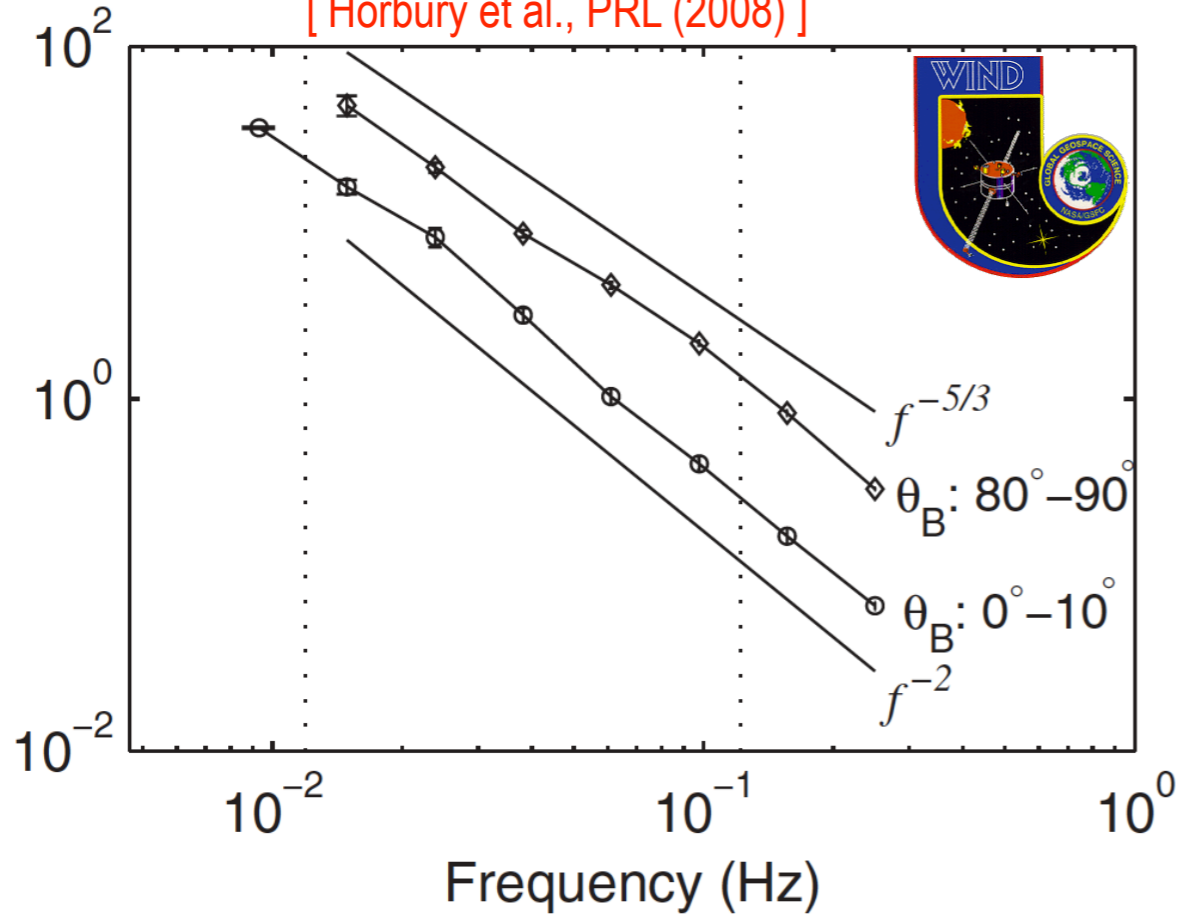
(Goldreich & Sridhar: *anisotropic MHD turbulence*)



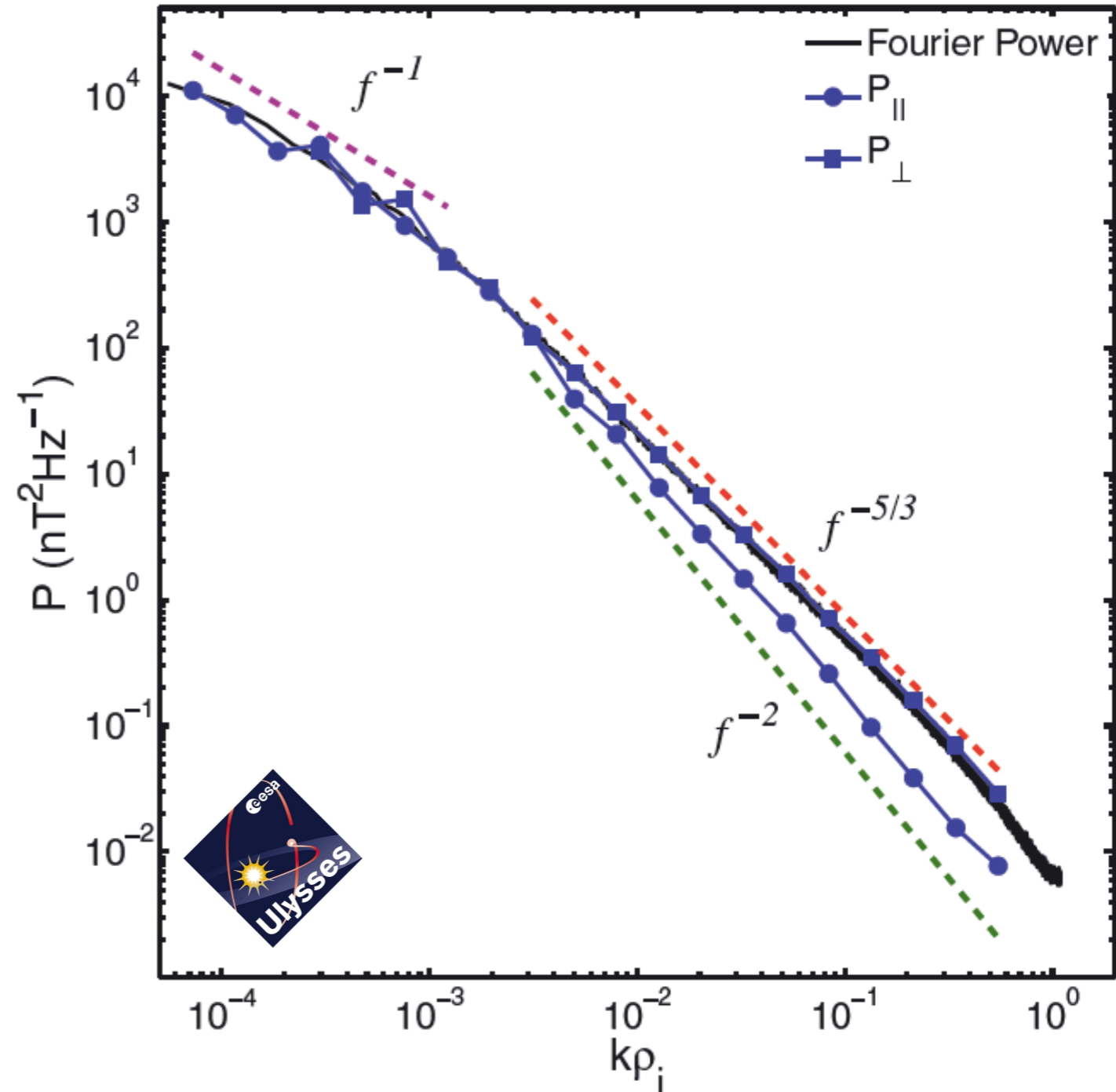
SW turbulence in the MHD range

Observations from WIND and Ulysses (and other spacecraft)

[Horbury et al., PRL (2008)]



[Wicks et al., MNRAS (2009)]



SW turbulence in the MHD range

Observations from WIND and Ulysses (and other spacecraft)

SW turbulence in the “inertial/MHD” range is essentially made of

***critically-balanced anisotropic cascade
of (mostly) Alfvénic-like fluctuations***

(à la Glodreich-Sridahr)

$$k_{\parallel} \propto k_{\perp}^{2/3}$$

$$E(k_{\perp}) \propto k_{\perp}^{-5/3}, \quad E(k_{\parallel}) \propto k_{\parallel}^{-2}$$

...what about the cascade at kinetic scales?

Tr(P) (arb. units)

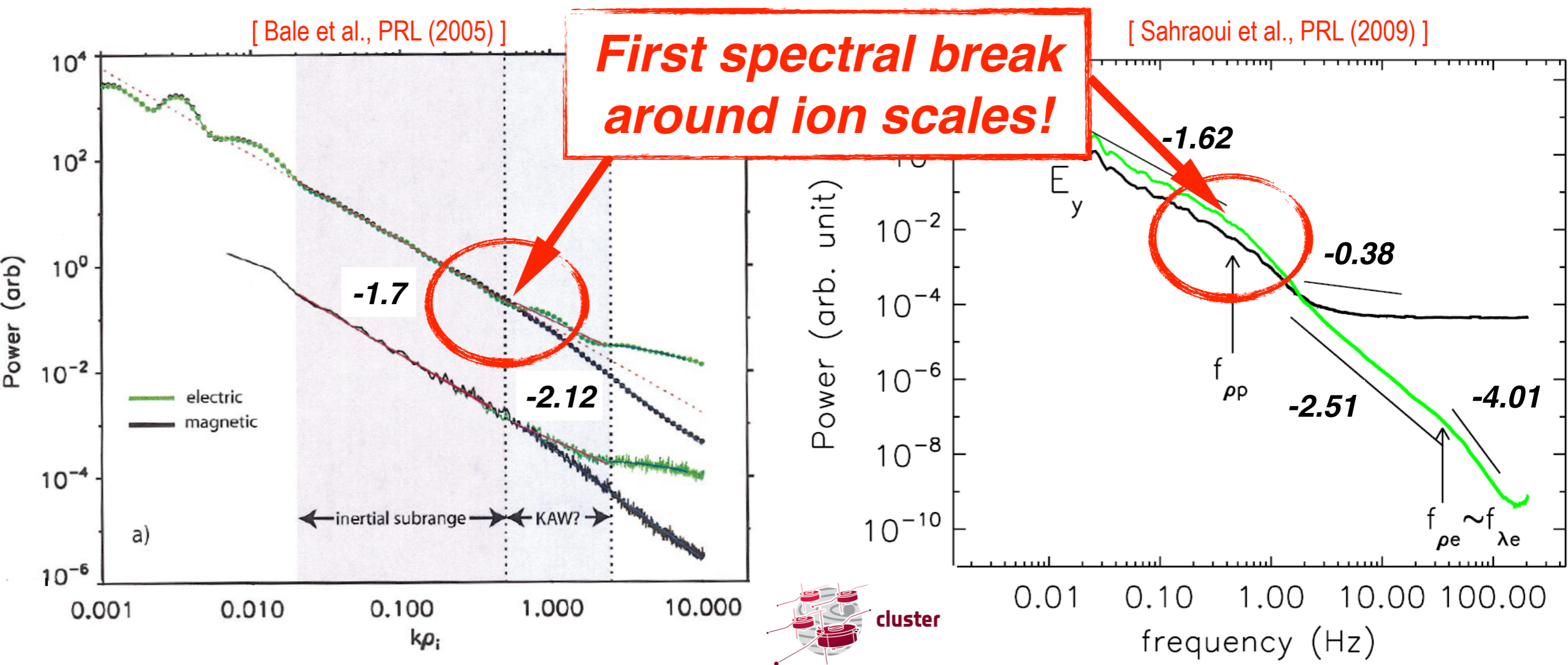
Spectral index

0 45 90 135 180

θ_B (degrees)

kp_i

SW turbulence beyond the MHD range

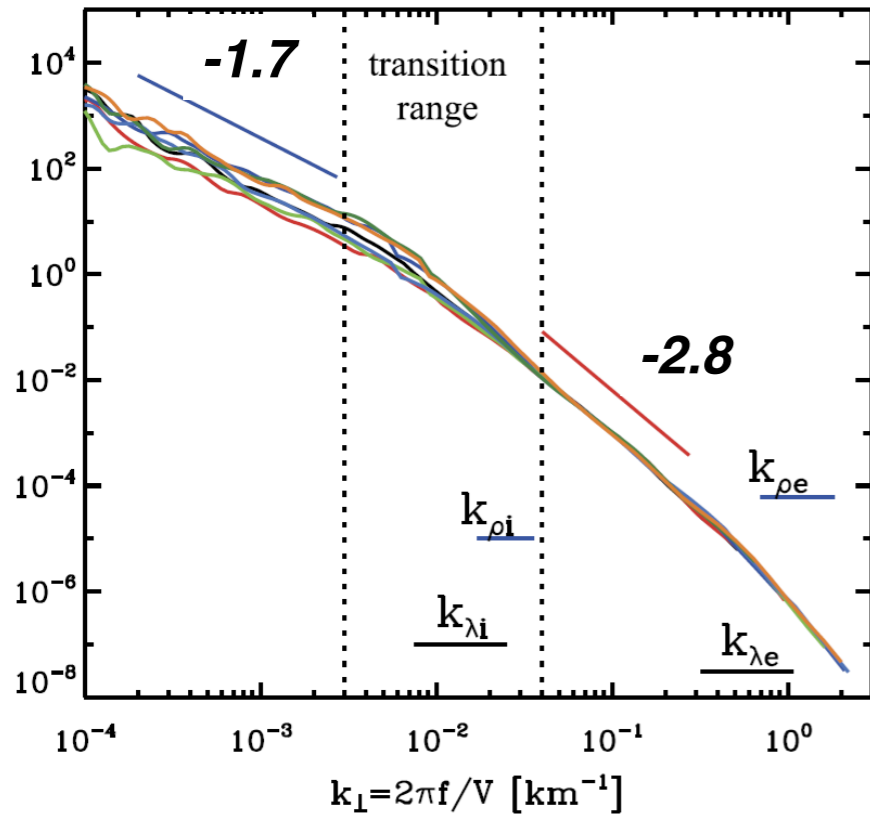


First observations of electromagnetic turbulent cascade at kinetic scales by Cluster:

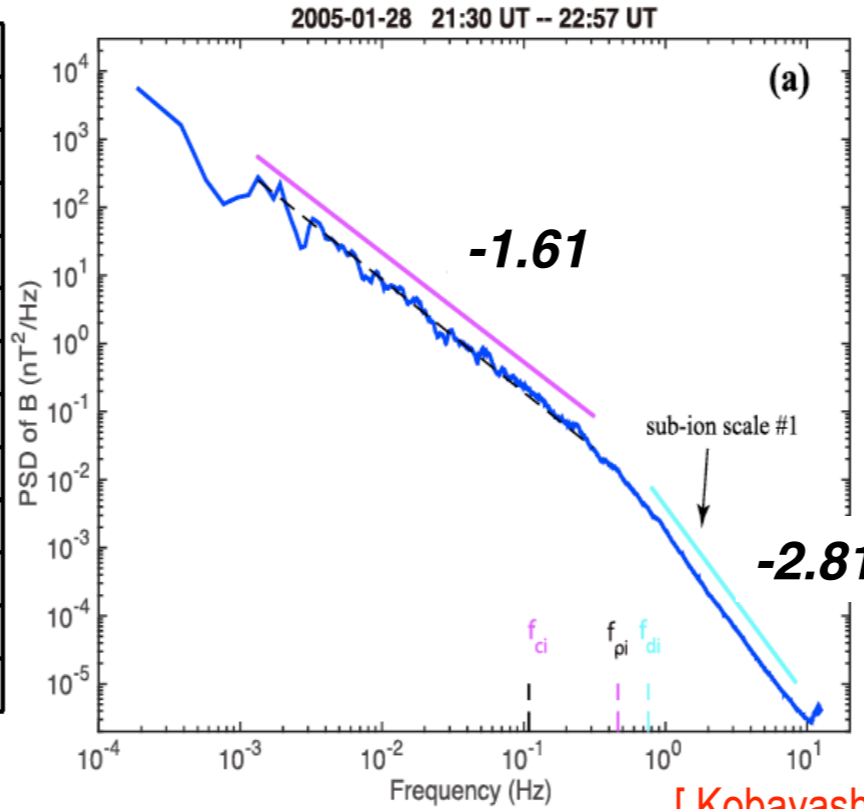
- **Spectral breaks at kinetic scales**
- **Steepening of magnetic spectrum**
- **Flattening of electric spectrum**

Universality of kinetic-range spectrum?

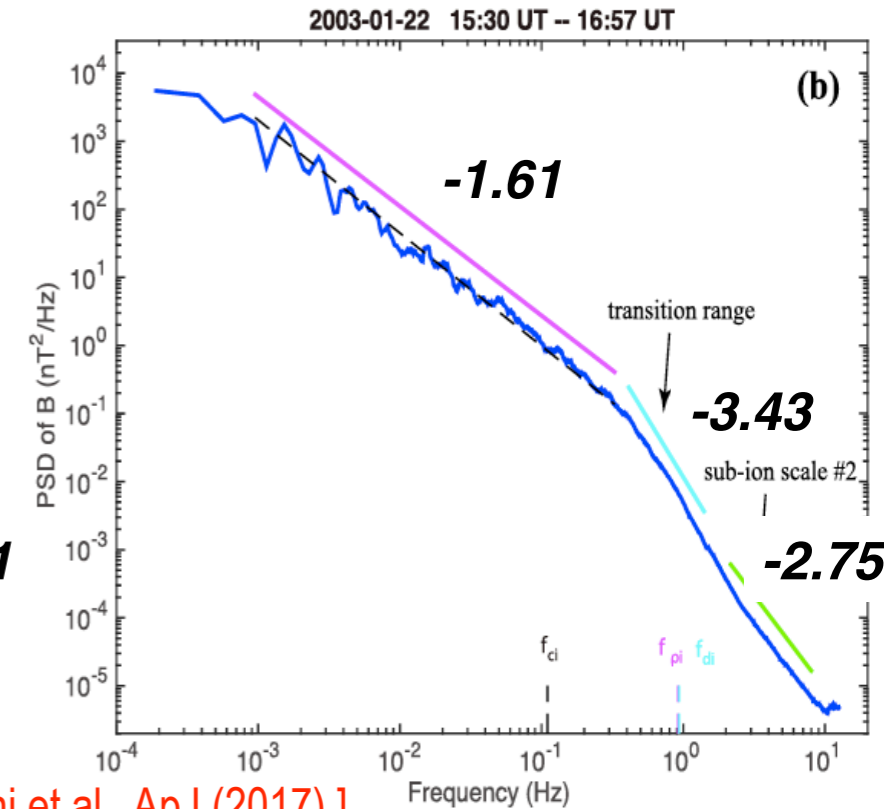
Solar Wind



[Alexandrova et al., SSR (2013)]

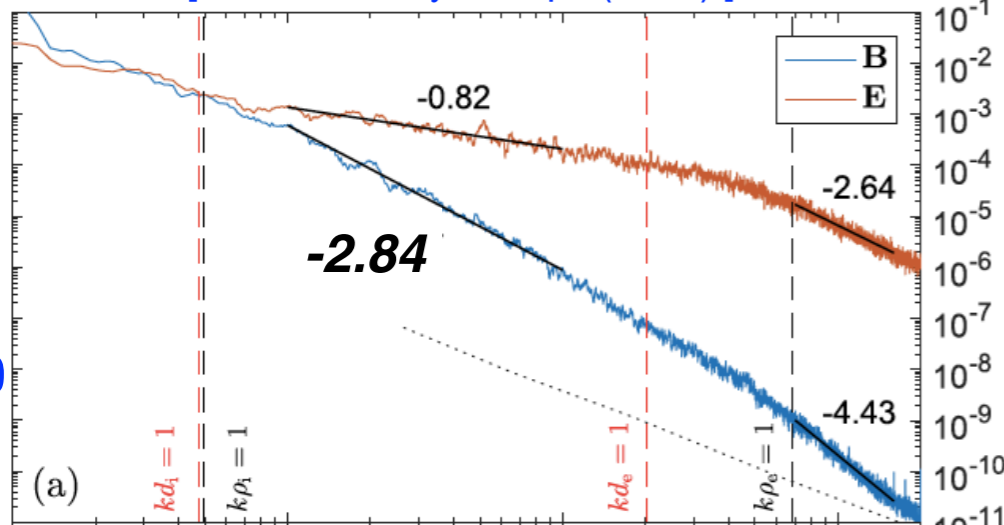


[Kobayashi et al., ApJ (2017)]

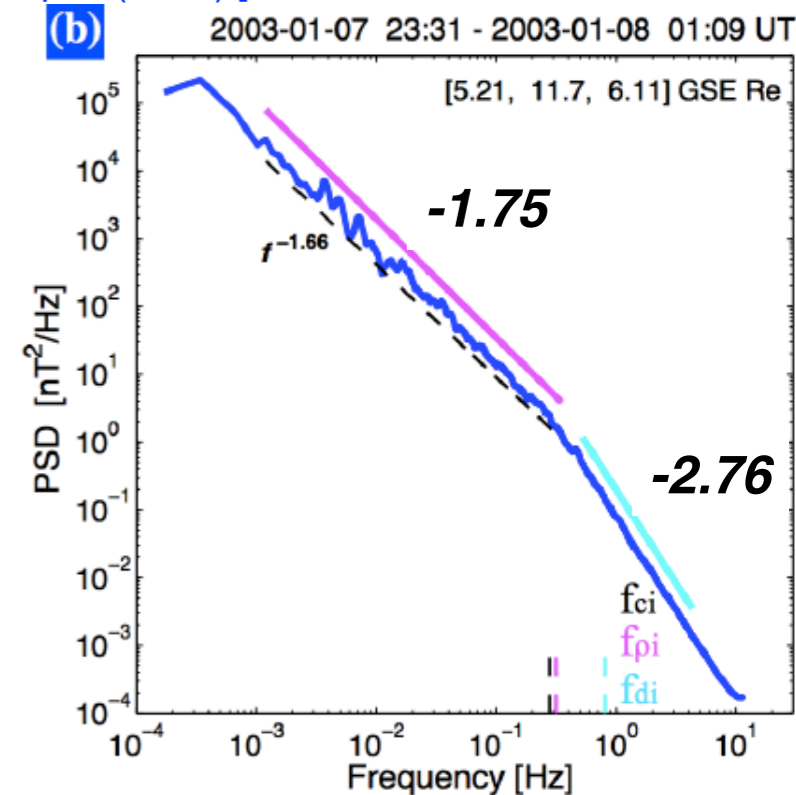
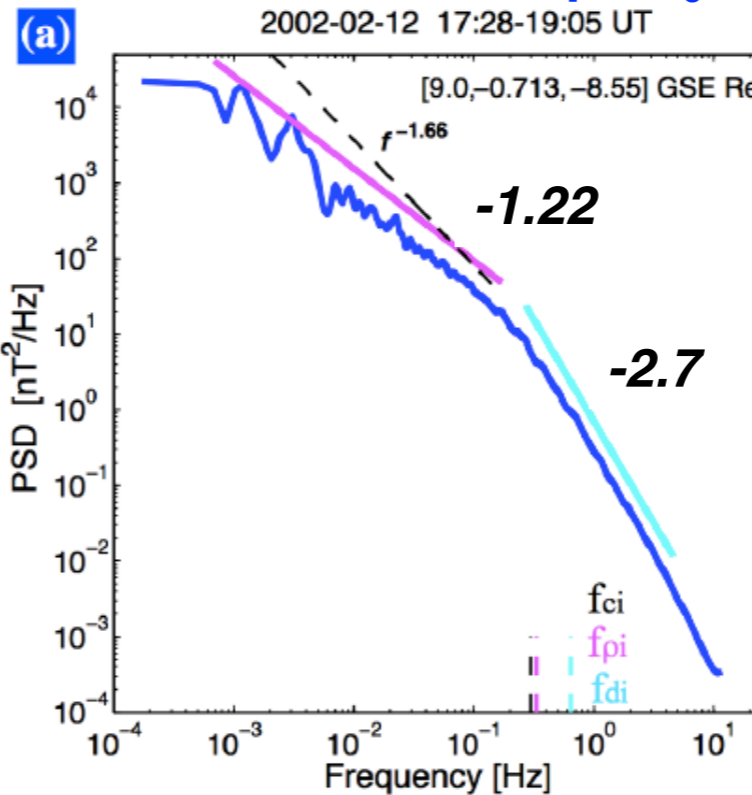


[Huang et al., ApJL (2017)]

Magnetosheath



[Chen & Boldyrev, ApJ (2017)]



Kinetic-range turbulence theories

Kinetic Alfvén wave (KAW) cascade

[see e.g. Schekochihin et al., ApJS (2009); Boldyrev et al., ApJ (2013)]

- B-spectrum $\sim k_{\perp}^{-7/3}$
- E-spectrum $\sim k_{\perp}^{-1/3}$
- Spectral anisotropy: $k_{\parallel} \sim k_{\perp}^{1/3}$

Whistler wave (WW) cascade

[see e.g. Galtier & Bhattacharjee, PoP (2003); Cho & Lazarian, ApJL (2004)]

- B-spectrum $\sim k_{\perp}^{-7/3}$
- E-spectrum $\sim k_{\perp}^{-1/3}$
- Spectral anisotropy: $k_{\parallel} \sim k_{\perp}^{1/3}$

Kinetic-range turbulence theories

Additional possible sources of steepening

• B

- Landau damping effects (within GK theory) [Howes et al., JGR (2008)]

• E

exponential corrections $\sim k_{\perp}^{-7/3} \exp(-F[\omega(\mathbf{k}), \gamma(\mathbf{k})])$

• S

- Compressibility effects [Alexandrova et al., ApJ (2008)]

B-spectrum $\sim k_{\perp}^{-7/3 - 2\xi}$

• B

- Intermittency effects [Boldyrev & Perez, ApJ (2012)]

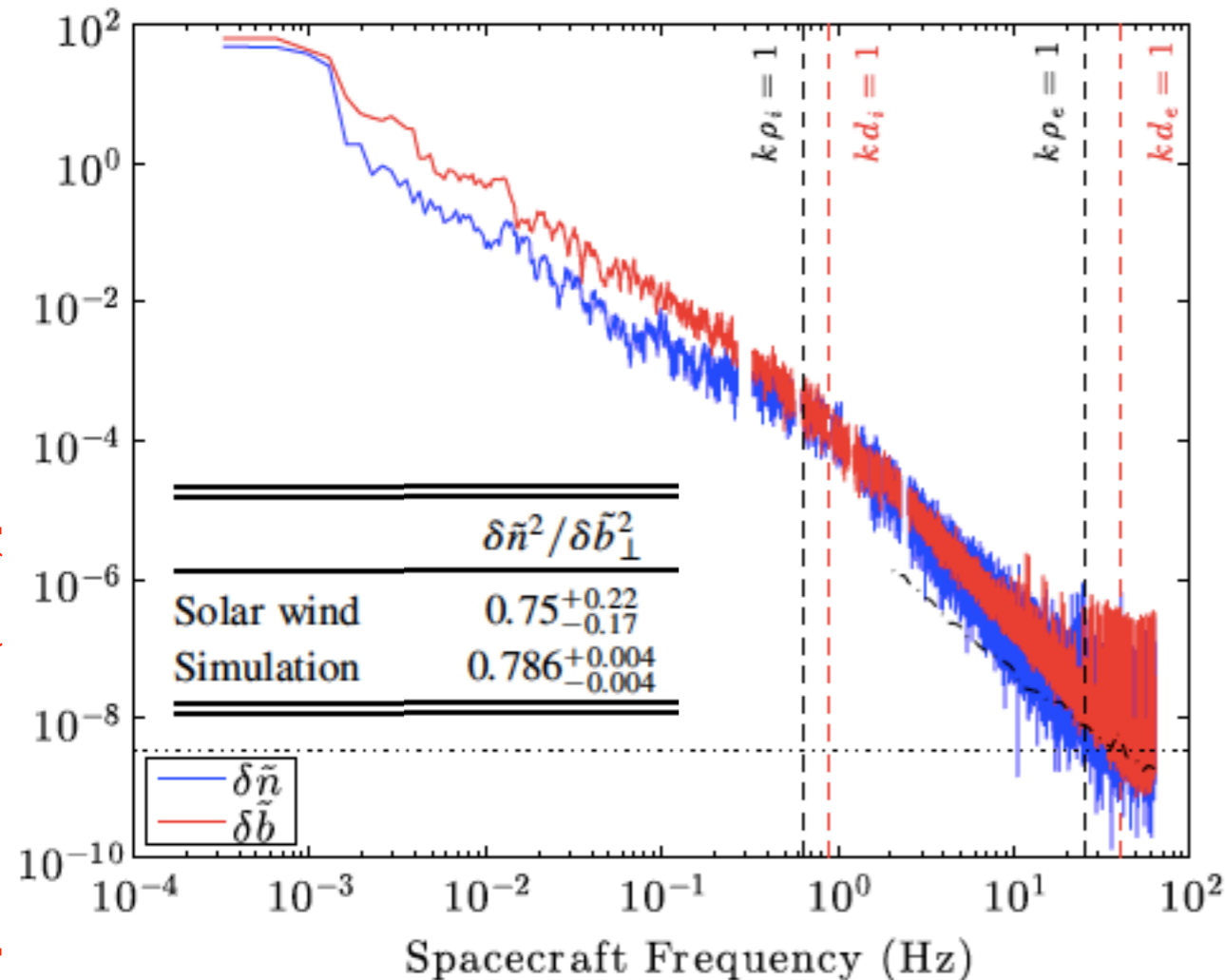
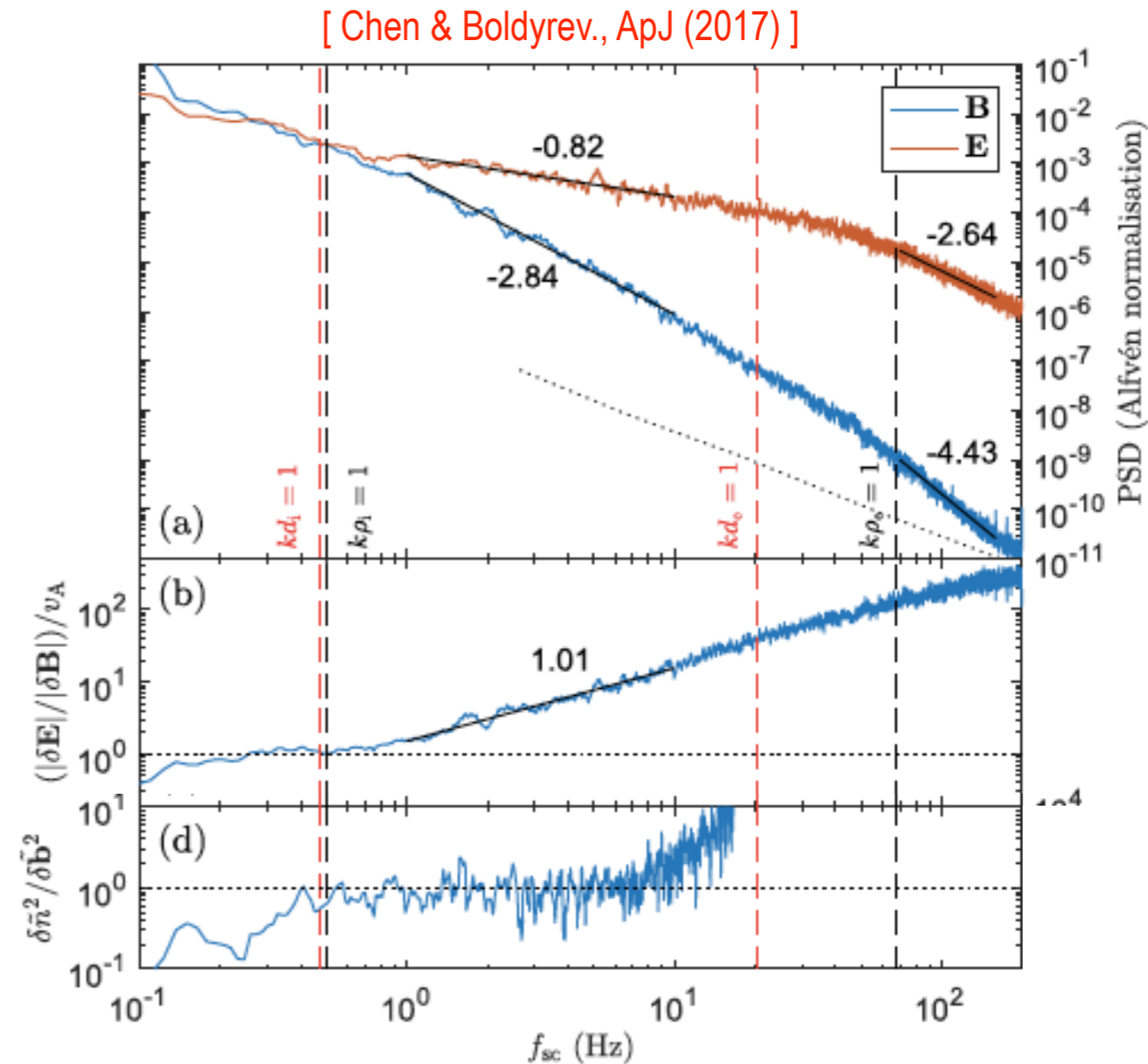
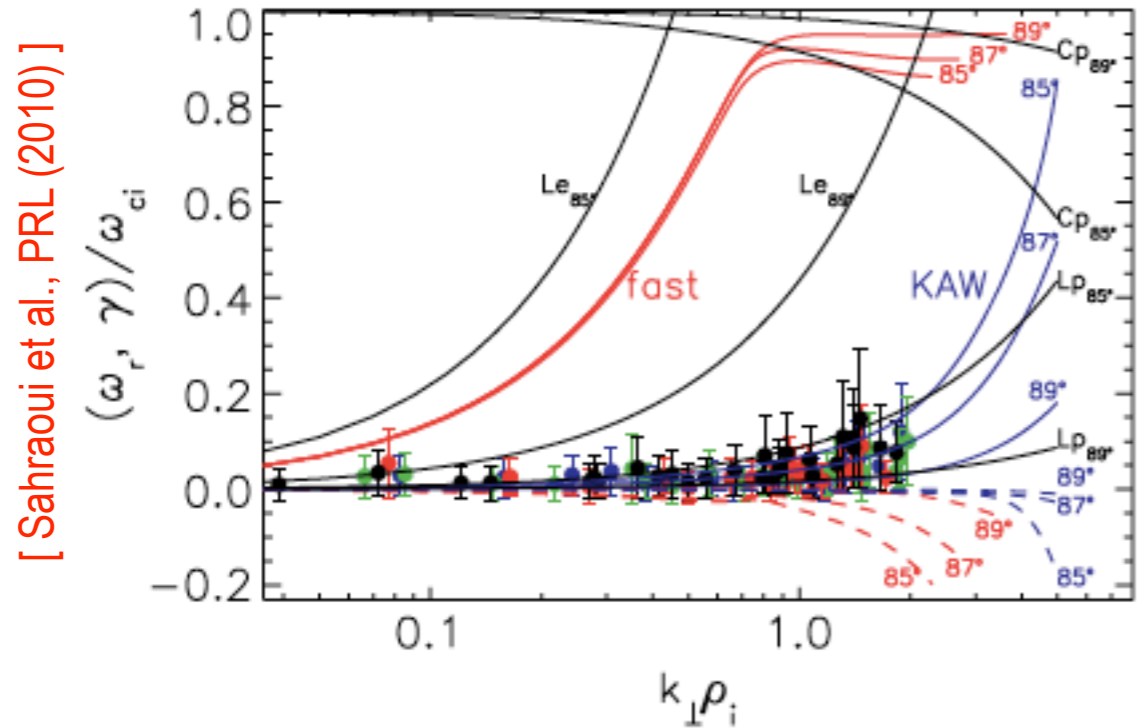
B-spectrum $\sim k_{\perp}^{-8/3}$; E-spectrum $\sim k_{\perp}^{-2/3}$; anisotropy $k_{\parallel} \sim k_{\perp}^{2/3}$

• E

- Nonlinearity parameter saturation (“weak vs strong..er”) [Passot & Sulem, ApJL (2015)]

• S

More kinetic-range turbulence observations



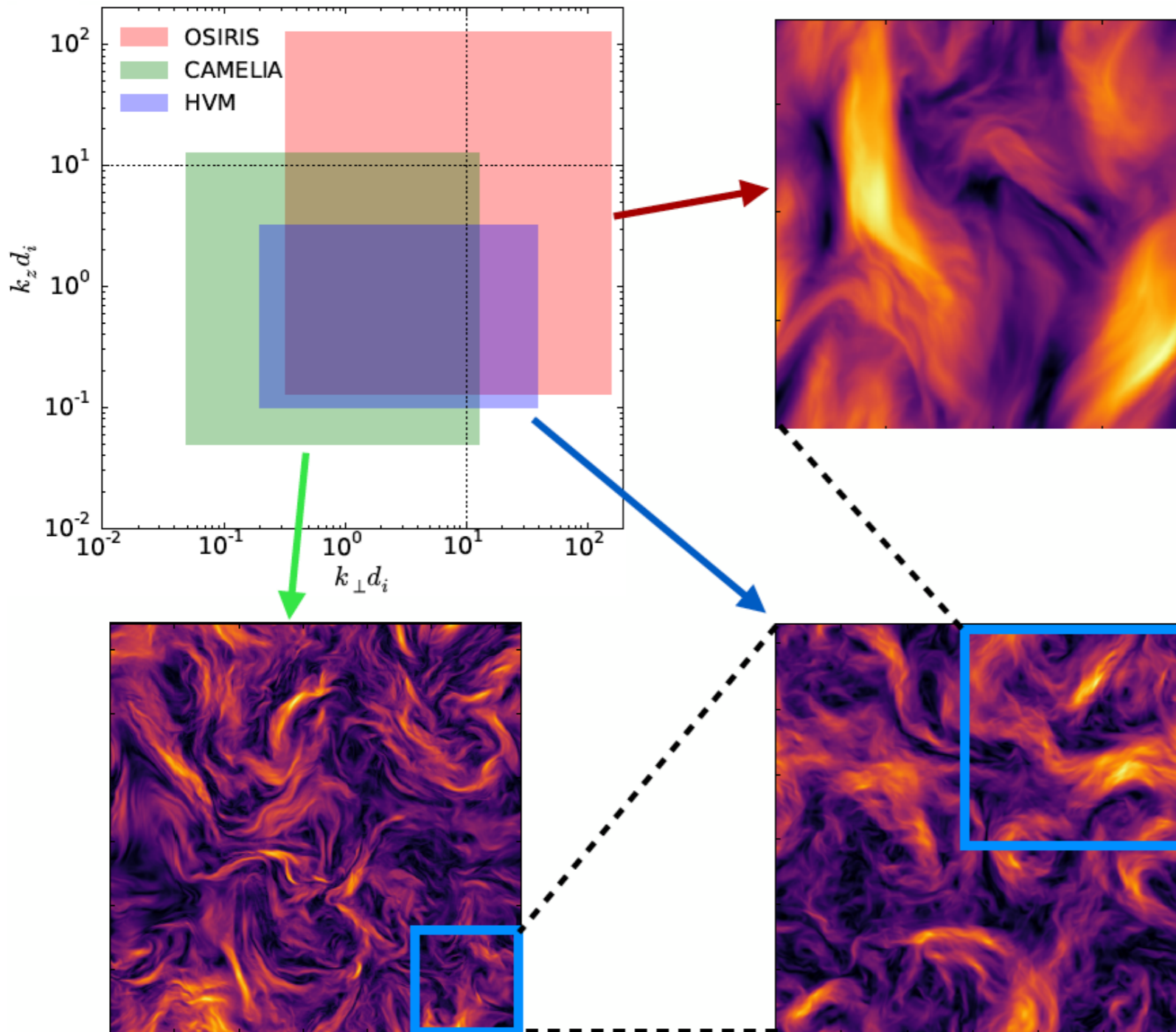
$$\delta \tilde{b} = \frac{\delta B}{B_0} \quad \delta \tilde{n} = \sqrt{\frac{\beta_i}{2} \left(1 + \frac{T_e}{T_i}\right) \left[1 + \frac{\beta_i}{2} \left(1 + \frac{T_e}{T_i}\right)\right]} \frac{\delta n}{n_0}$$

observations are overall consistent with *kinetic-Alfvén-wave (KAW) turbulence*

Spectral anisotropy: a solution, after all?

Understanding sub-ion-range turbulence: a multi-model, collaborative effort

[Cerri, Grosej & Franci, FSPAS (2019)]



👉 Different injection properties

at “MHD scales”:

- freely decaying Alfvénic fluctuations
- freely decaying compressive B fluctuations
- continuous Alfvénic injection (“driven”)

👉 Different models and numerical

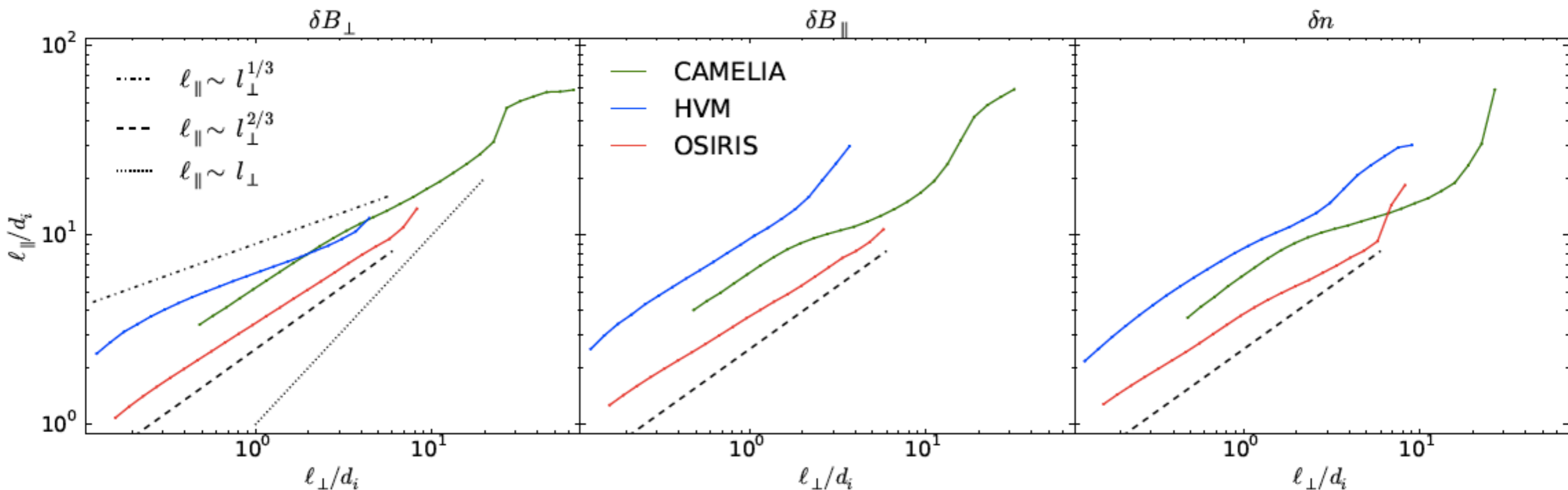
methods employed:

- hybrid-PIC w/o electron inertia
- hybrid-Vlasov w/ electron inertia
- full PIC

Spectral anisotropy: a solution, after all?

With high-angular-resolution, multi-point structure functions every simulation eventually agrees on the spectral anisotropy of (almost) each quantity!

[Cerri, Grosej & Franci, FSPAS (2019)]



sub-ion-scale anisotropy: $\ell_{\parallel} \sim \ell_{\perp}^{2/3}$

(polarisation properties of sub-ion-scale fluctuations are also consistent with kinetic-Alfvén-wave turbulence — not shown here)

Spectral anisotropy: a solution, after all?

Observations & simulations of turbulent fluctuations in the “sub-ion range” are overall consistent with

**“intermittency corrected”
kinetic-Alfvén-wave (KAW) turbulence**

BUT this is not the end of the story:

Reconnection & turbulence as tightly entwined processes
→ **idea of “reconnection-mediated turbulence” for sub-ion range**

see, e.g.,

Cerri & Califano, NJP (2017) [simulations]

Franci, Cerri, et al., ApJL (2017) [simulations]

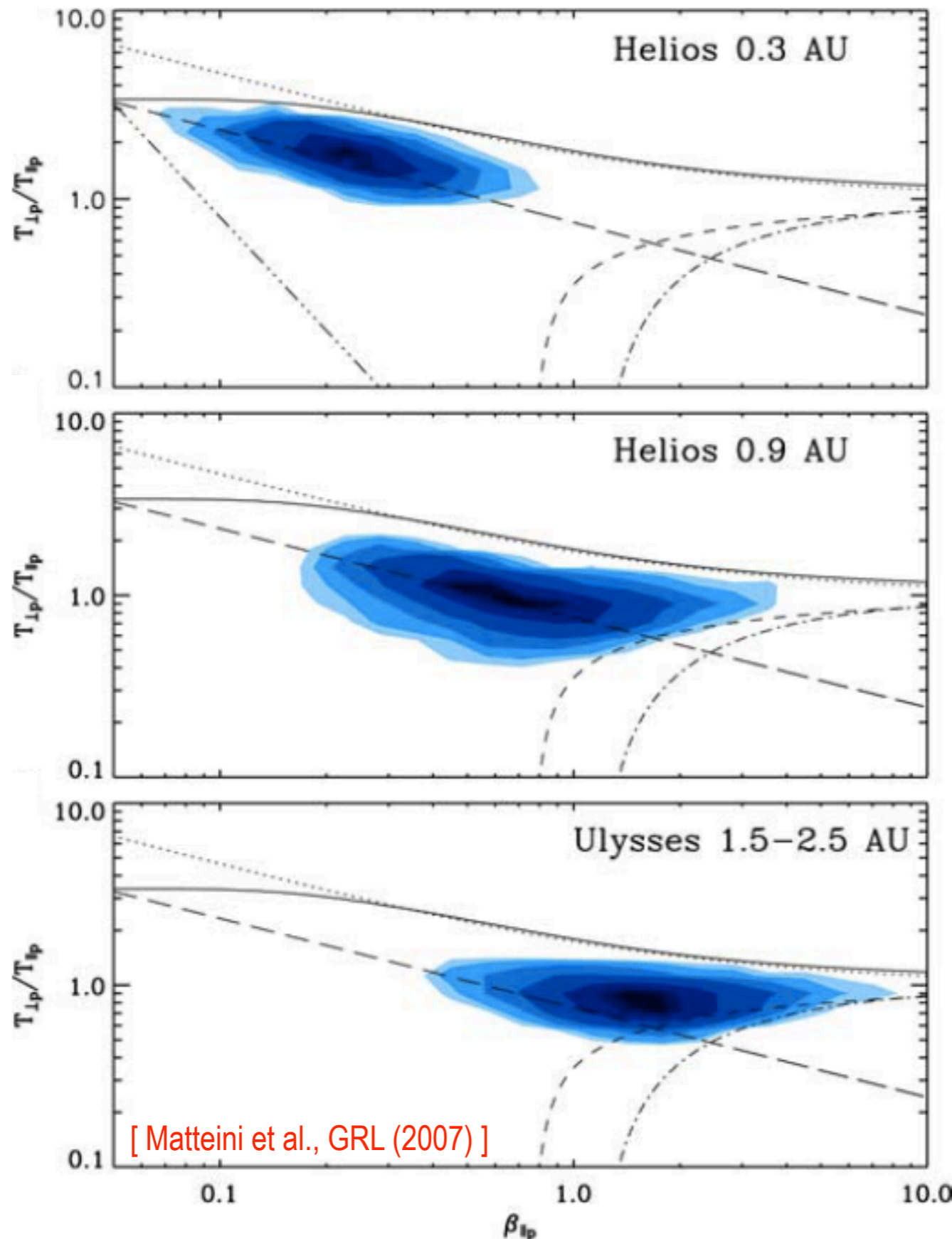
Loureiro & Boldyrev, ApJ (2017) [theory]

Mallet, Schekochihin & Chandran, JPP (2017) [theory]

Vech et al., ApJL (2018) [observations]

...what about turbulent heating?

Temperature evolution in turbulent SW



- ▶ Proton temperature parallel and perpendicular to the local magnetic field **does not follow an adiabatic evolution**
- ▶ Other processes must dominate the thermal evolution of the turbulent SW plasma (“**turbulent heating**”)
- ▶ Turbulent heating seems to **preferentially heat the protons in the direction perpendicular to B**

How turbulent energy finds its path to dissipation in a “collisionless” plasma?

Turbulent cascades in velocity space

A “collisionless” plasma enjoys the whole phase-space playground!

LINEAR PHASE MIXING

due to ballistic response of f :

$$\delta f \sim \exp(-ik_{\parallel}v_{\parallel}t)$$

slower than its nonlinear counterpart
(at scales below the ion gyro-radius)

→ presumably mainly **along B_0** (“parallel”)

and more important at “**large**” **perpendicular scales**:

$$k_{\perp}\rho_i \lesssim 1$$

NON-LINEAR PHASE MIXING

de-correlation of v_{\perp} -structures of f
due to de-correlated k_{\perp} -fluctuations:

$$\frac{\delta v_{\perp}}{v_{\text{th}i}} \sim \frac{1}{\rho_i} \left| \frac{v_{\perp}}{\Omega_i} - \frac{v'_{\perp}}{\Omega_i} \right| \sim \frac{1}{k_{\perp}\rho_i} \ll 1$$

(typically) faster than its linear counterpart, when active:

→ occurring only **perpendicular to B_0**

and only **below the ion gyro-radius**:

$$k_{\perp}\rho_i \gg 1$$

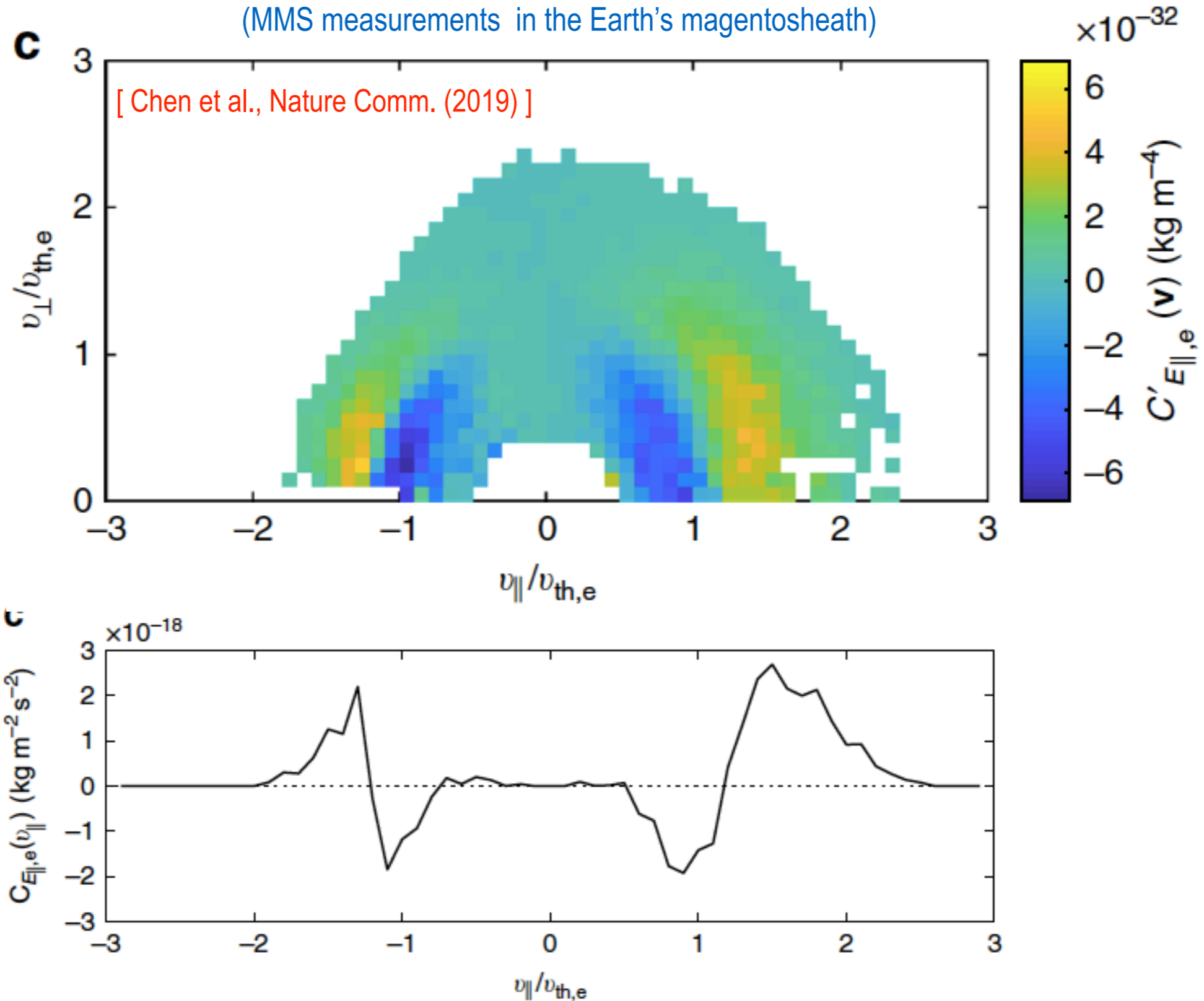


[Schekochihin et al., ApJS (2009)]

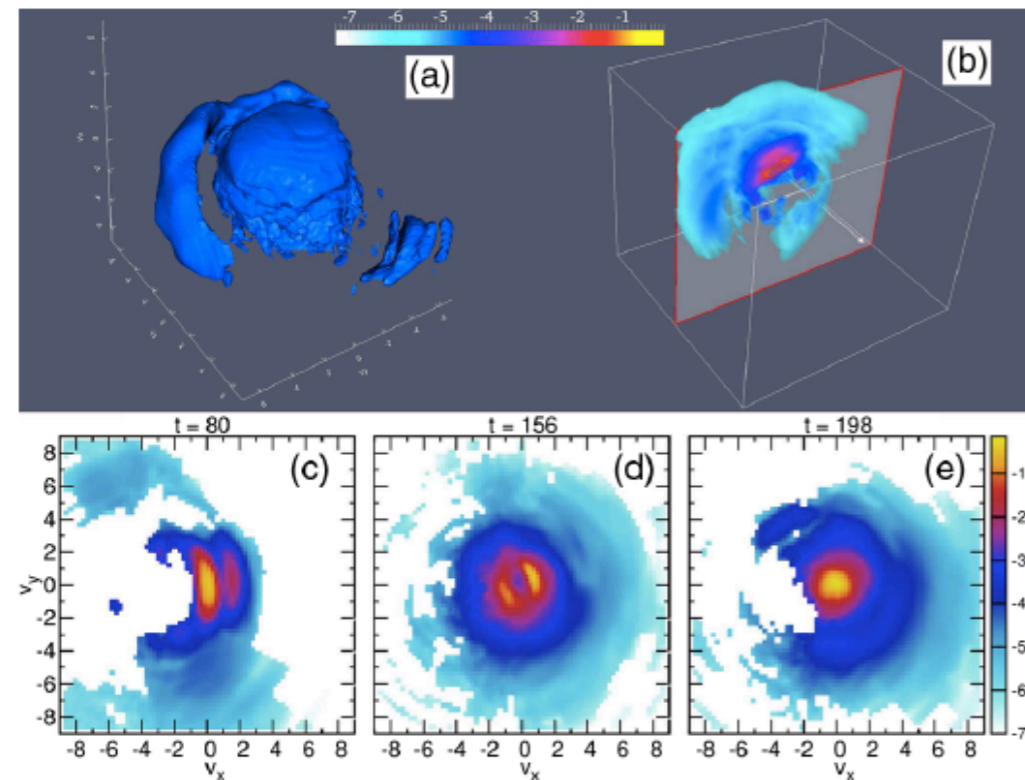
Landau damping of turbulent fluctuations

First evidence of Landau damping from in-situ data

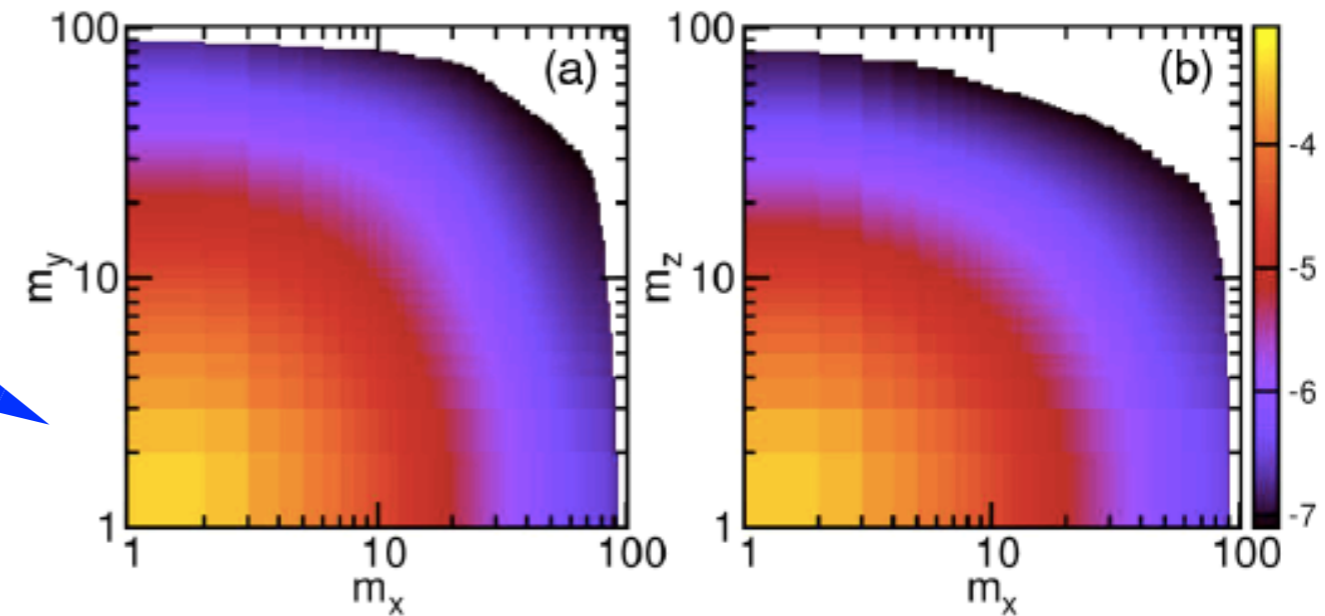
(MMS measurements in the Earth's magnetosheath)



MMS observation of v-space cascades

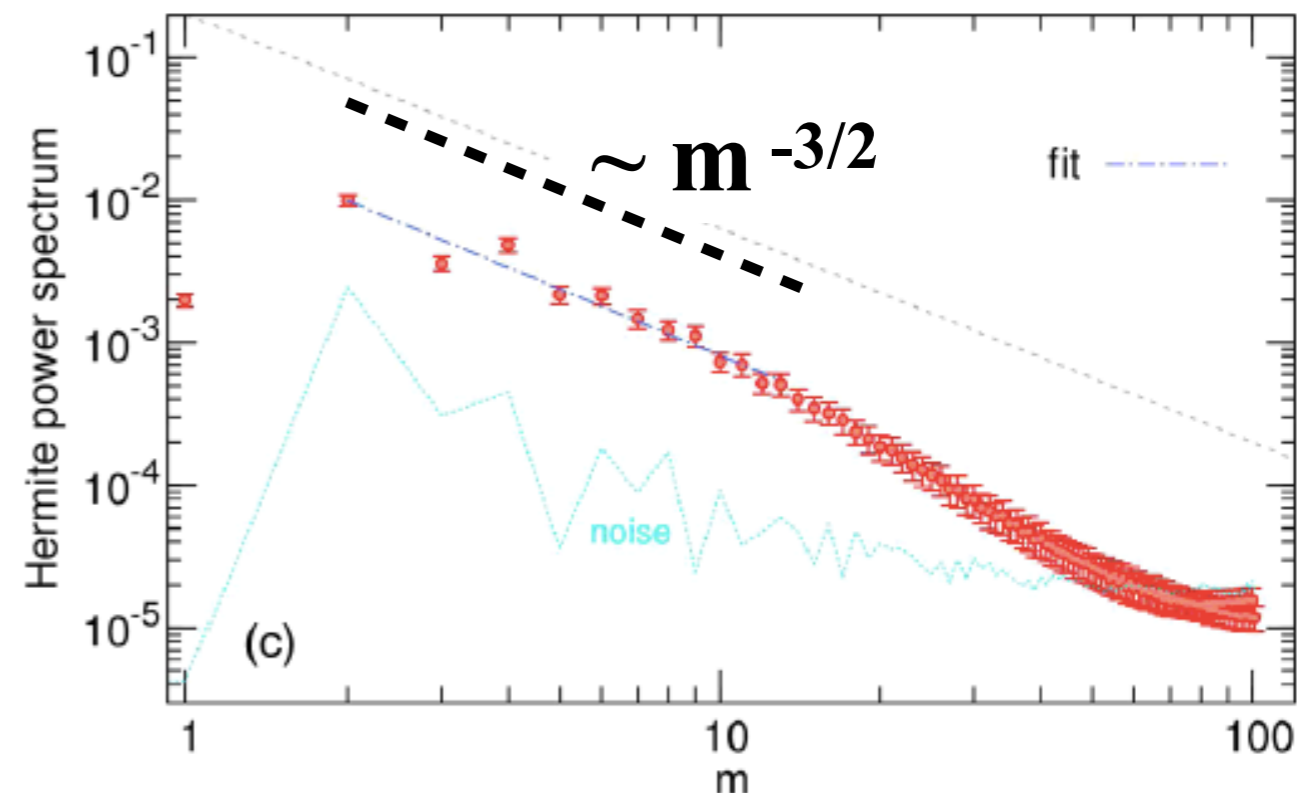


[Servidio et al., PRL (2017)]



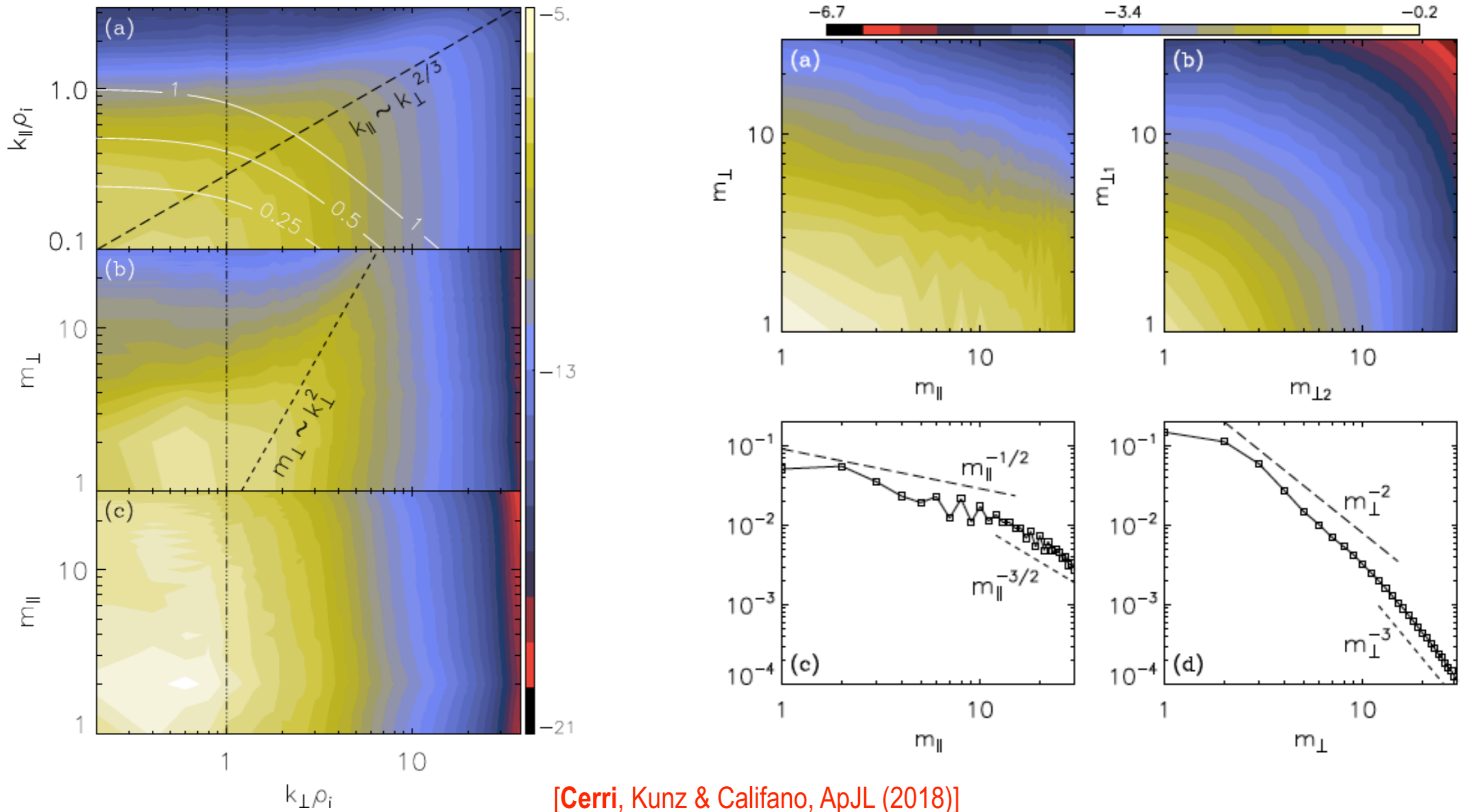
First evidence of a cascade in velocity space from in-situ data!

(measured by MMS in the Earth's magnetosheath)



Multiple players are allowed!

Anisotropic cascade of ion free-energy fluctuations in 6D phase space

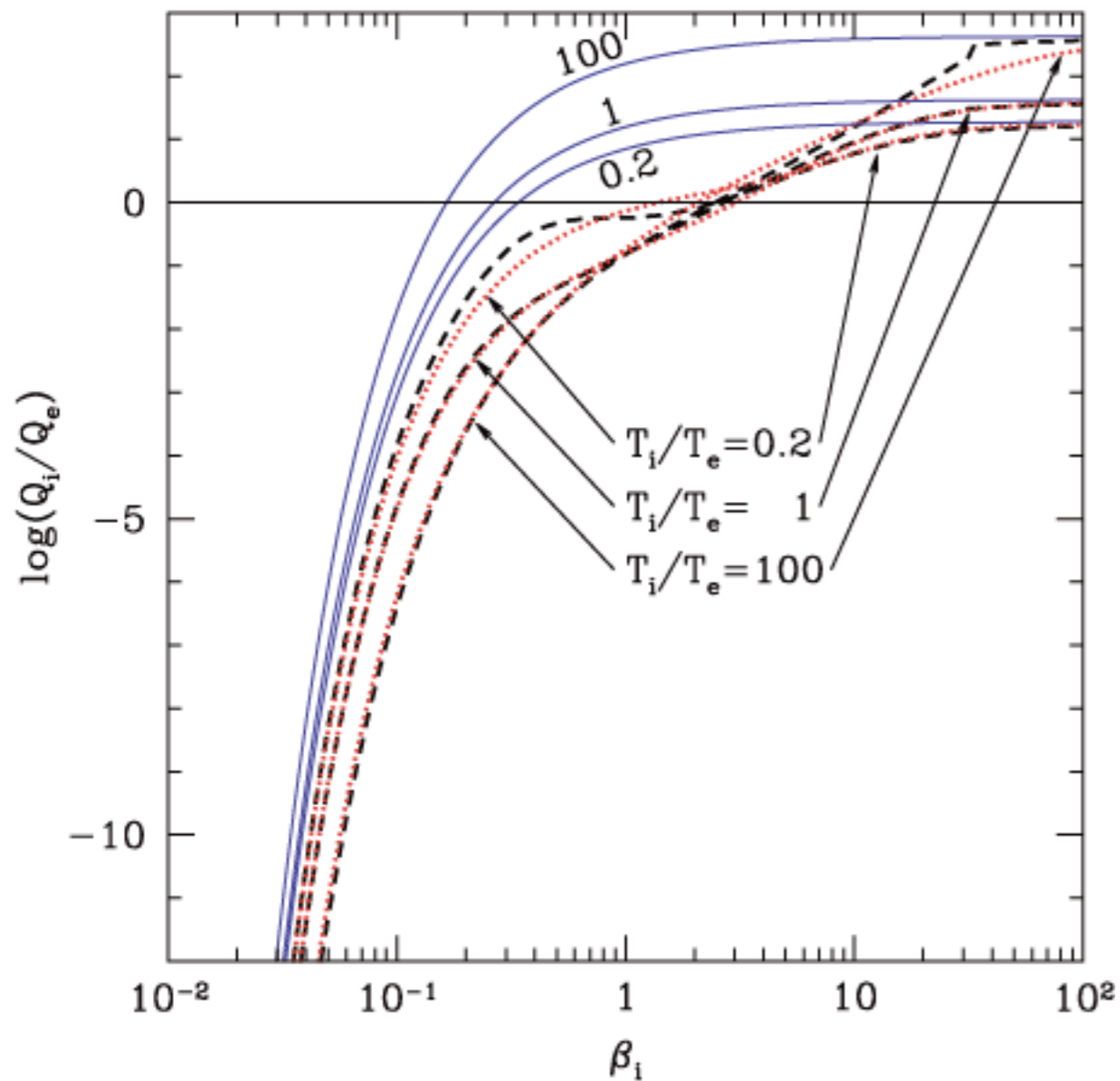


→ *different mechanisms can be simultaneously at play*

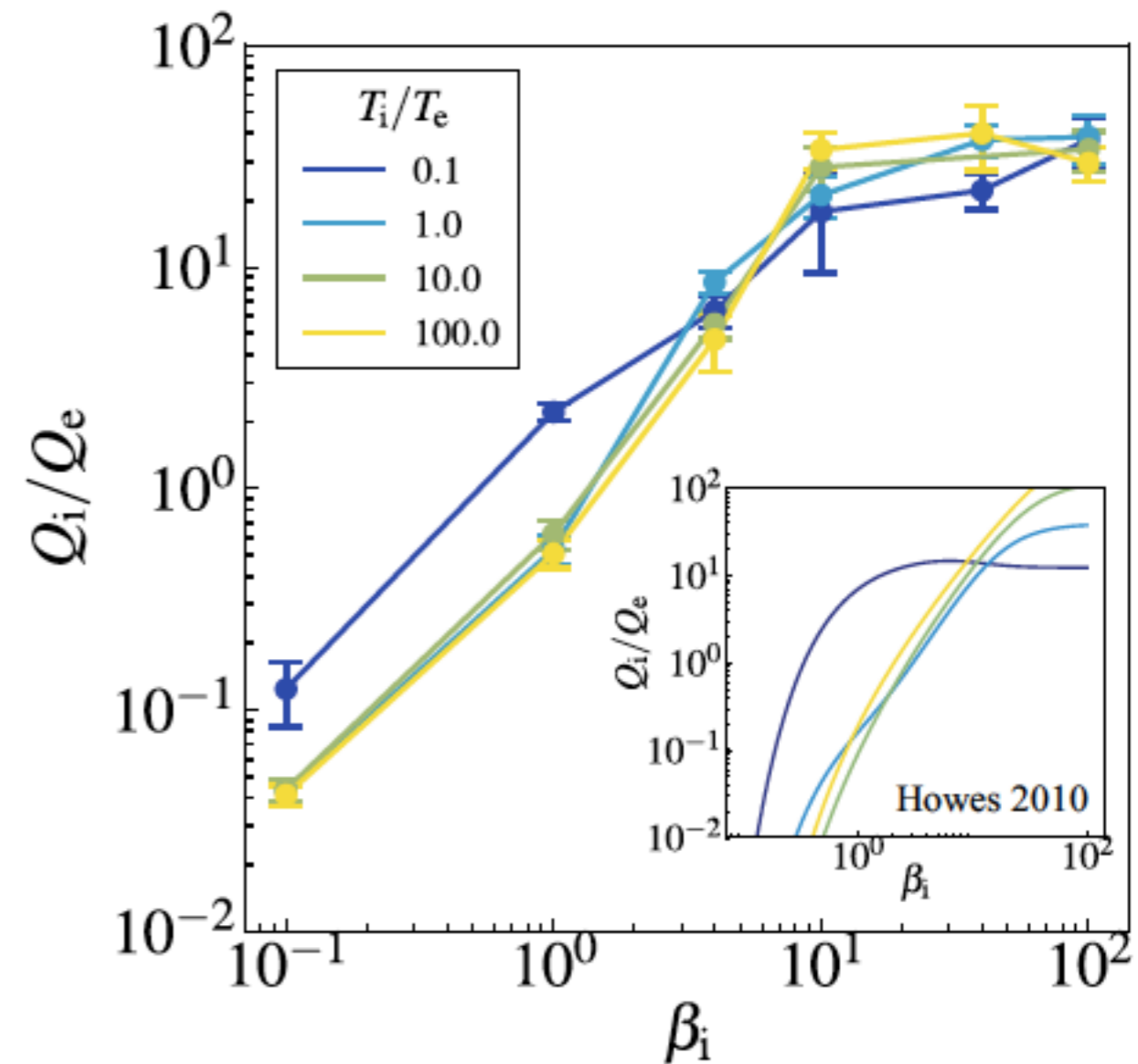
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Turbulent heating from gyro-kinetic (GK) damping rates

$$Q_s(k_{\perp}) = 2C_1^{3/2} C_2 (\bar{\gamma}_s / \bar{\omega}) \epsilon(k_{\perp}) / k_{\perp}$$



[Howes, MNRAS (2010)]



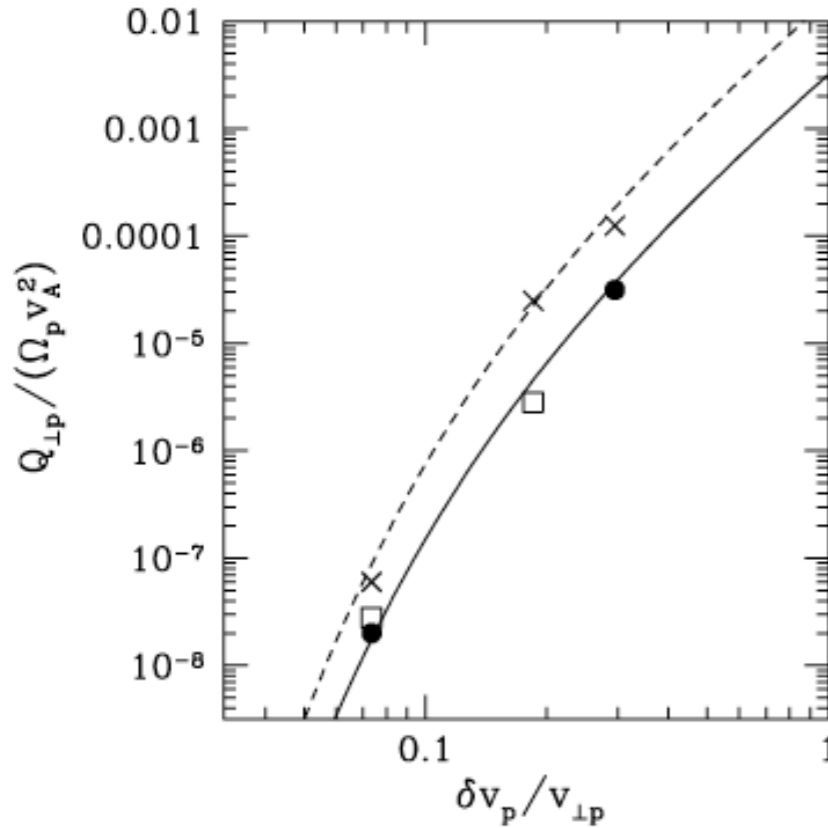
[Kawazura et al., PNAS (2019)]

Finite-amplitude fluctuations at ion gyroscale

Stochastic heating in low-frequency turbulent fluctuations

$$Q_{\perp} = \frac{c_1(\delta v_i)^3}{\rho_i} \exp\left(-\frac{c_2}{\varepsilon_i}\right) \quad \varepsilon_i = \frac{\delta v_i}{v_{\perp i}} \simeq \beta^{-1/2} \delta B_p / B_0$$

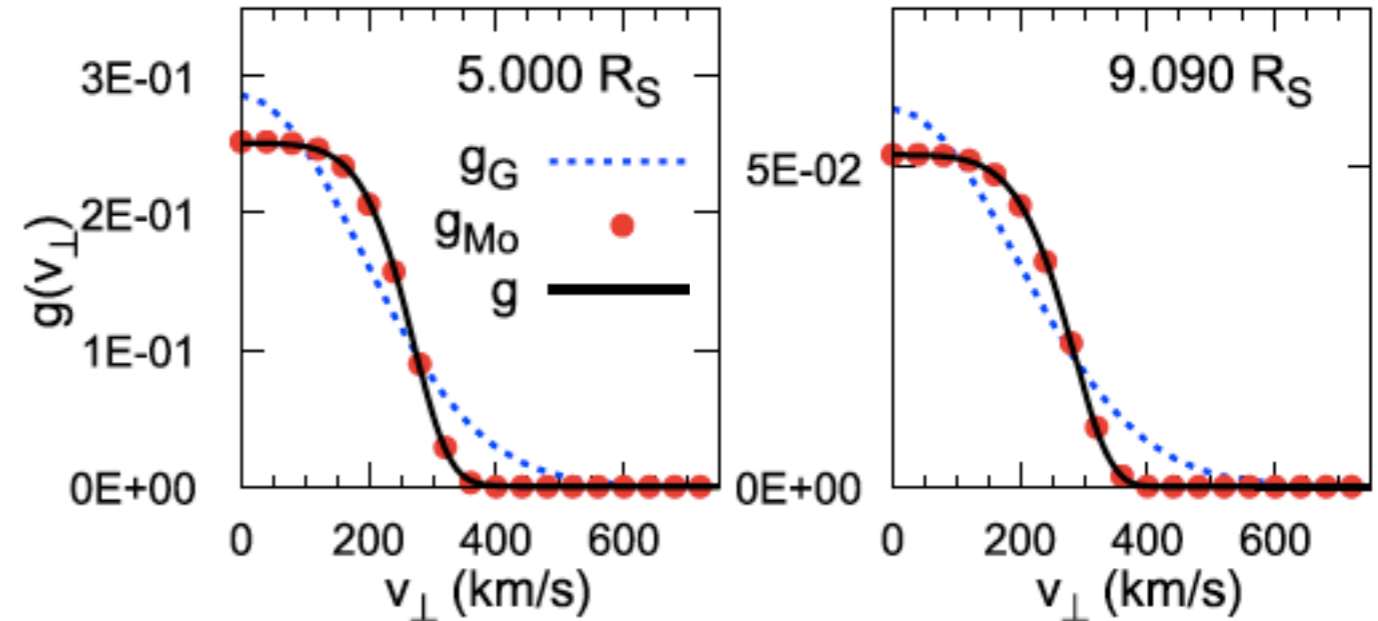
[Chandran et al., ApJ (2010)]



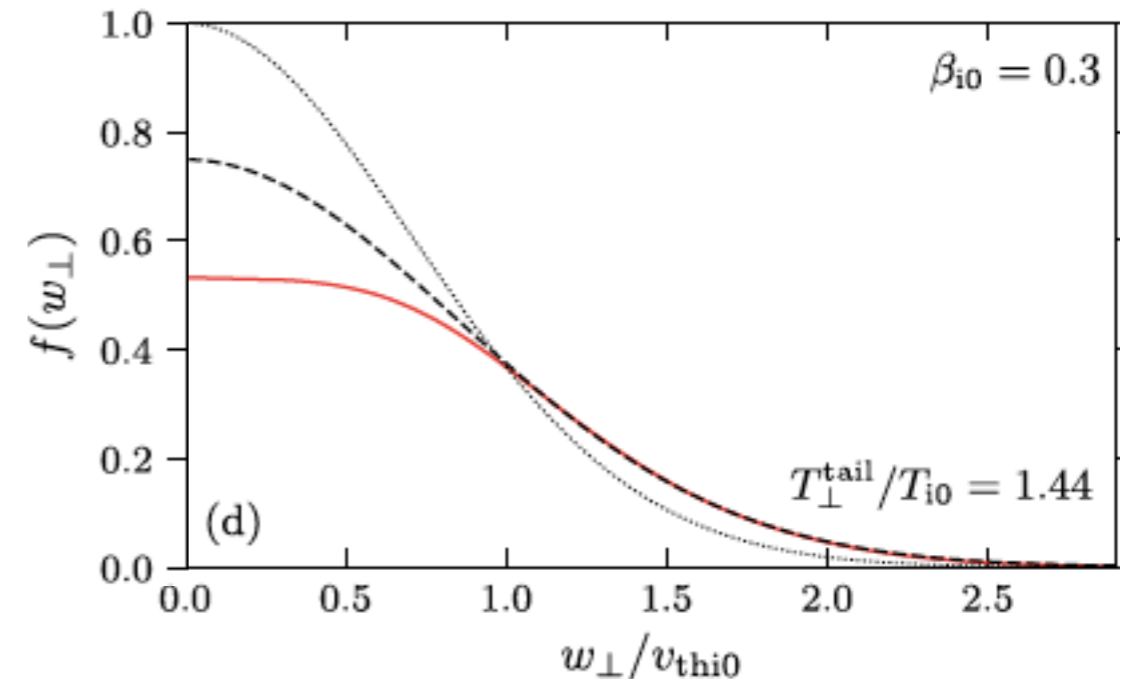
$$\Gamma = C_K^{-3/2} \left(\frac{\delta v_p}{\rho_p}\right) \left(\frac{\delta B_p}{B_0}\right)^2 v_A^2$$

$$\frac{Q_{\perp p}}{\Gamma} = 3.0 \exp\left(-\frac{0.34}{\varepsilon_p}\right)$$

[Klein & Chandran, ApJ (2016)]

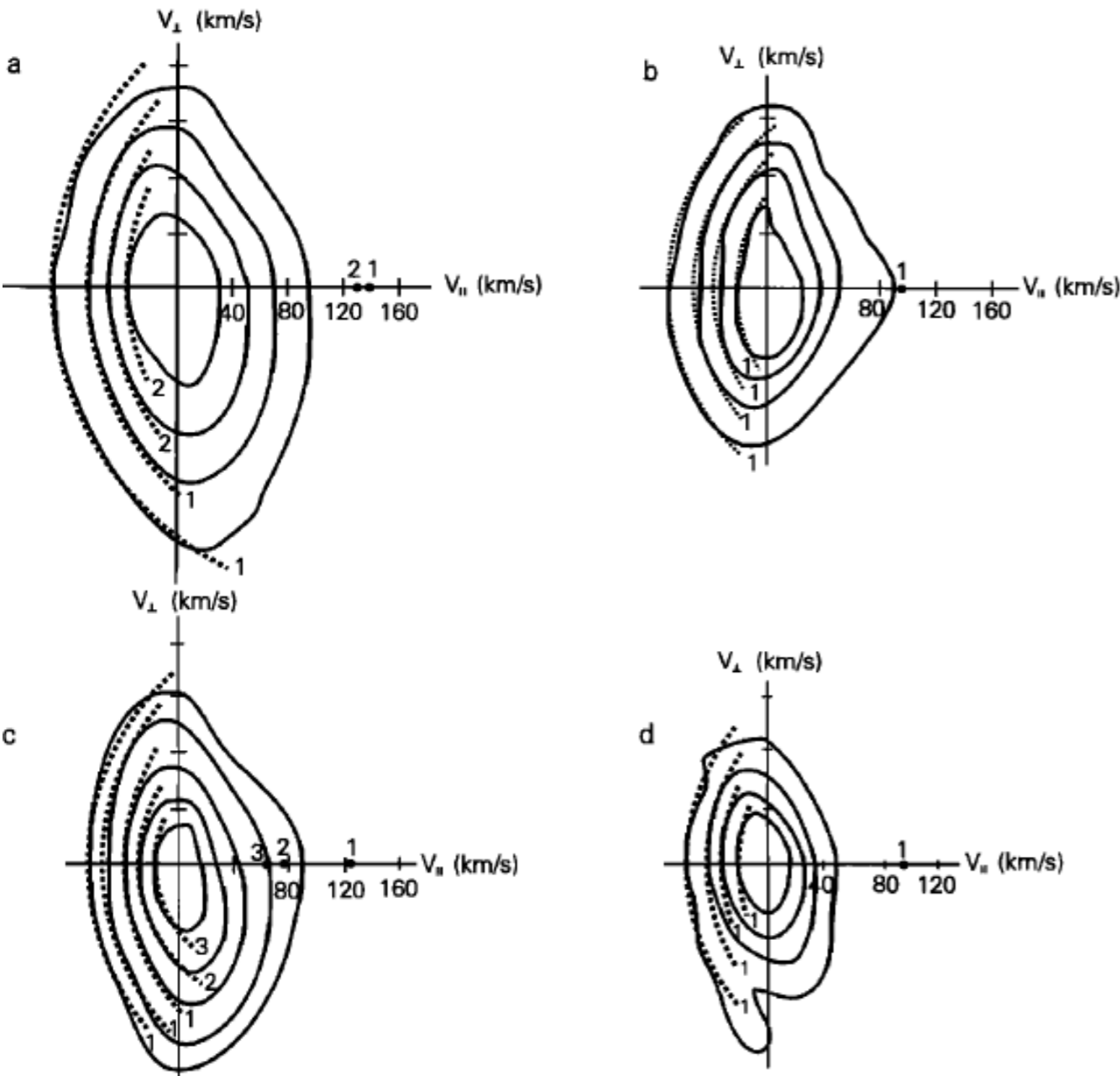


[Arzamasskiy et al., ApJ (2019)]

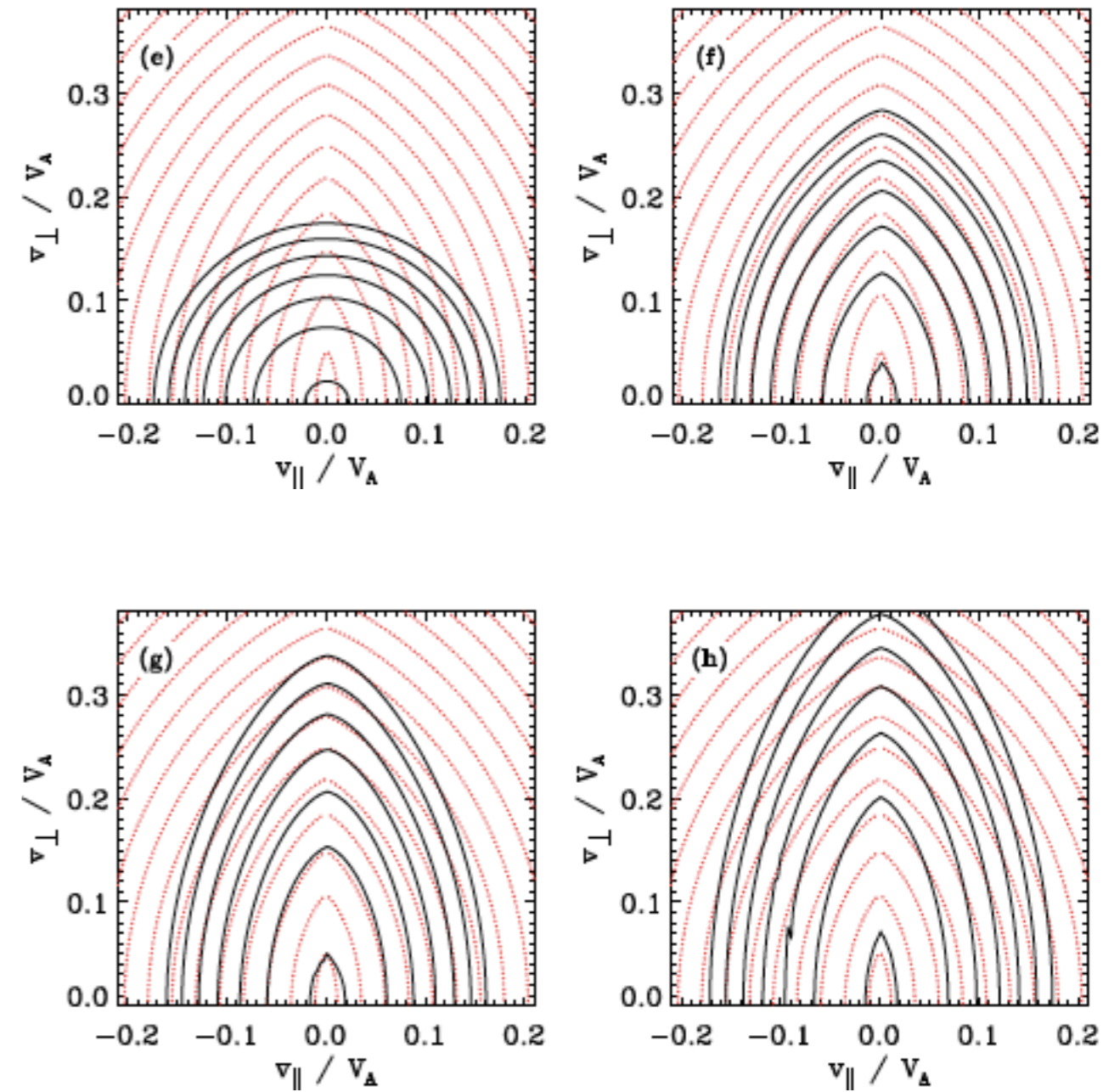


“high-frequency” fluctuations

Ion-cyclotron heating



[Marsch & Tu, JGR (2001)]

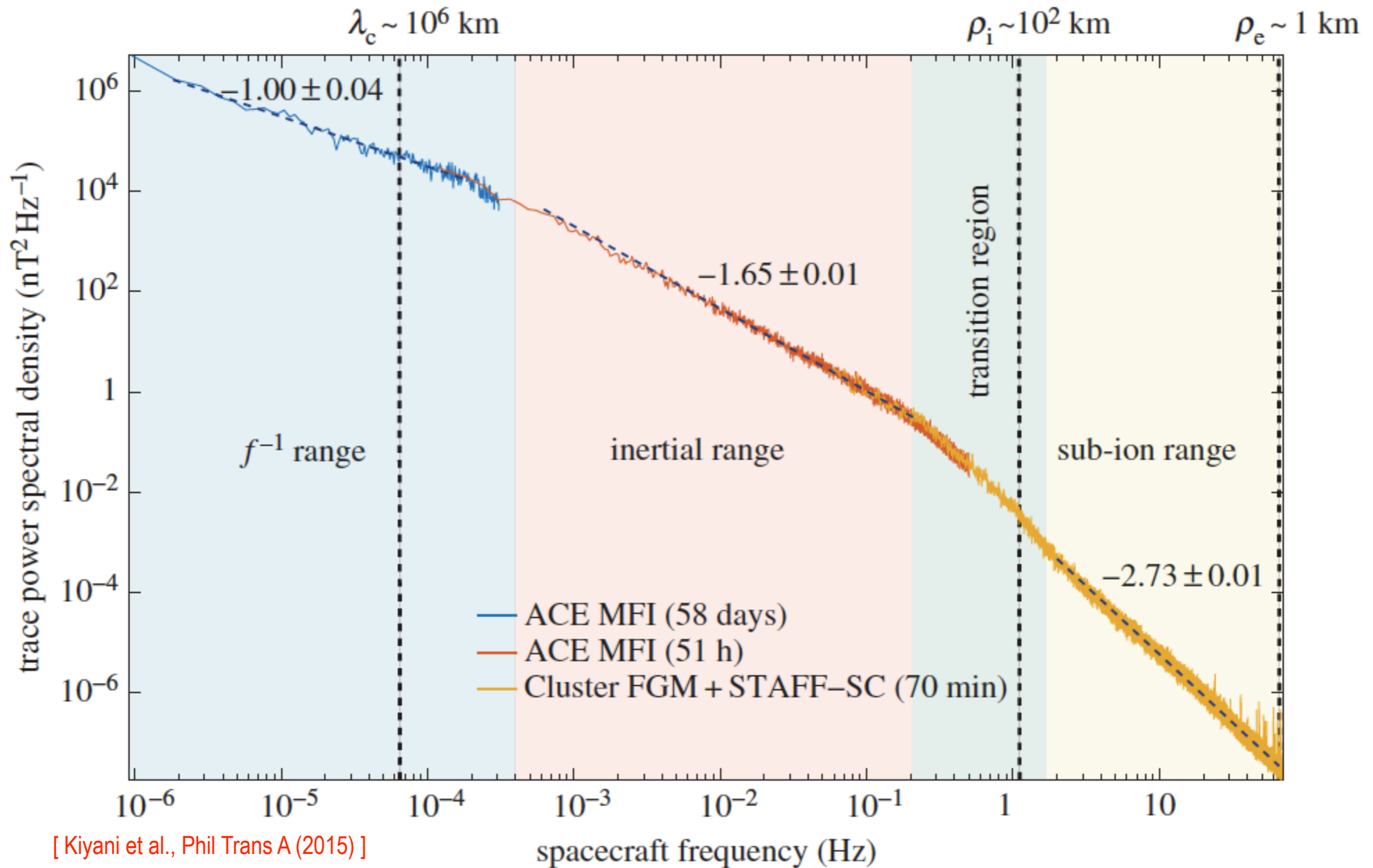


[Cranmer, ApJS (2014)]

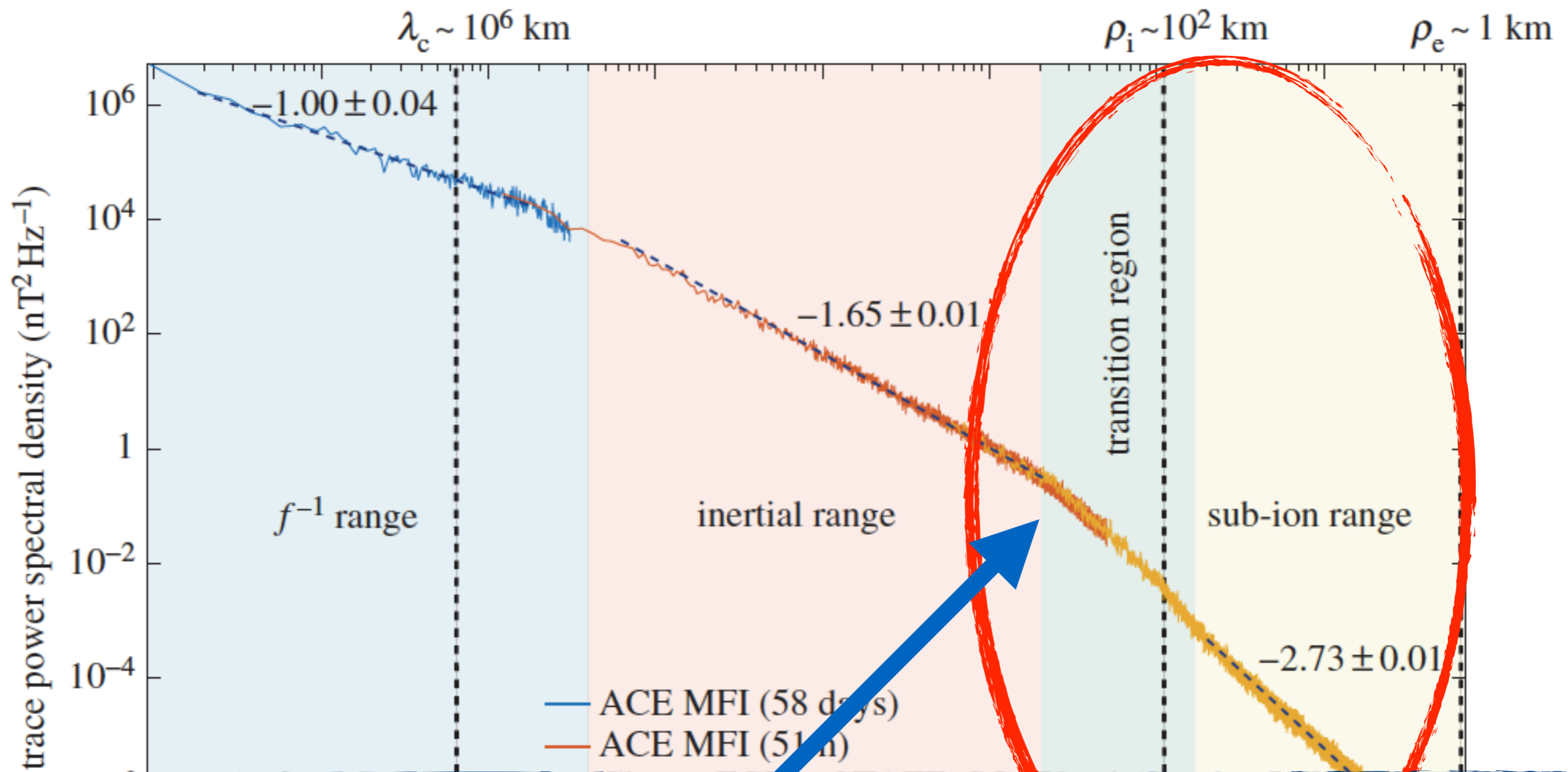
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The standard picture of SW turbulence



The standard picture of SW turbulence



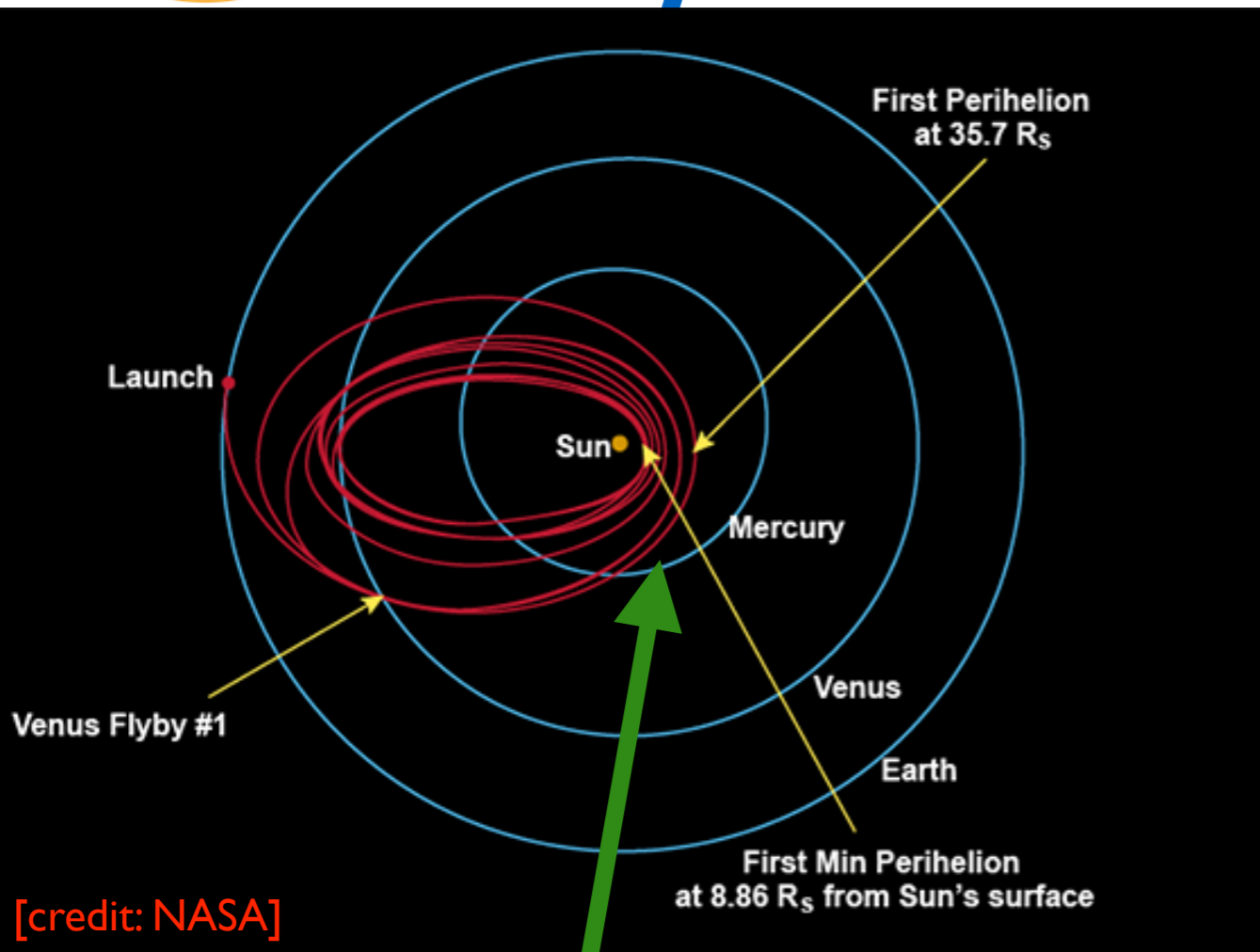
(We think that) What the system “chooses” in terms of turbulent cascade and turbulent heating is occurring across the transition region, and perhaps in part of the sub-ion range
(e.g., what kinetic cascade and heating “channels” get activated)

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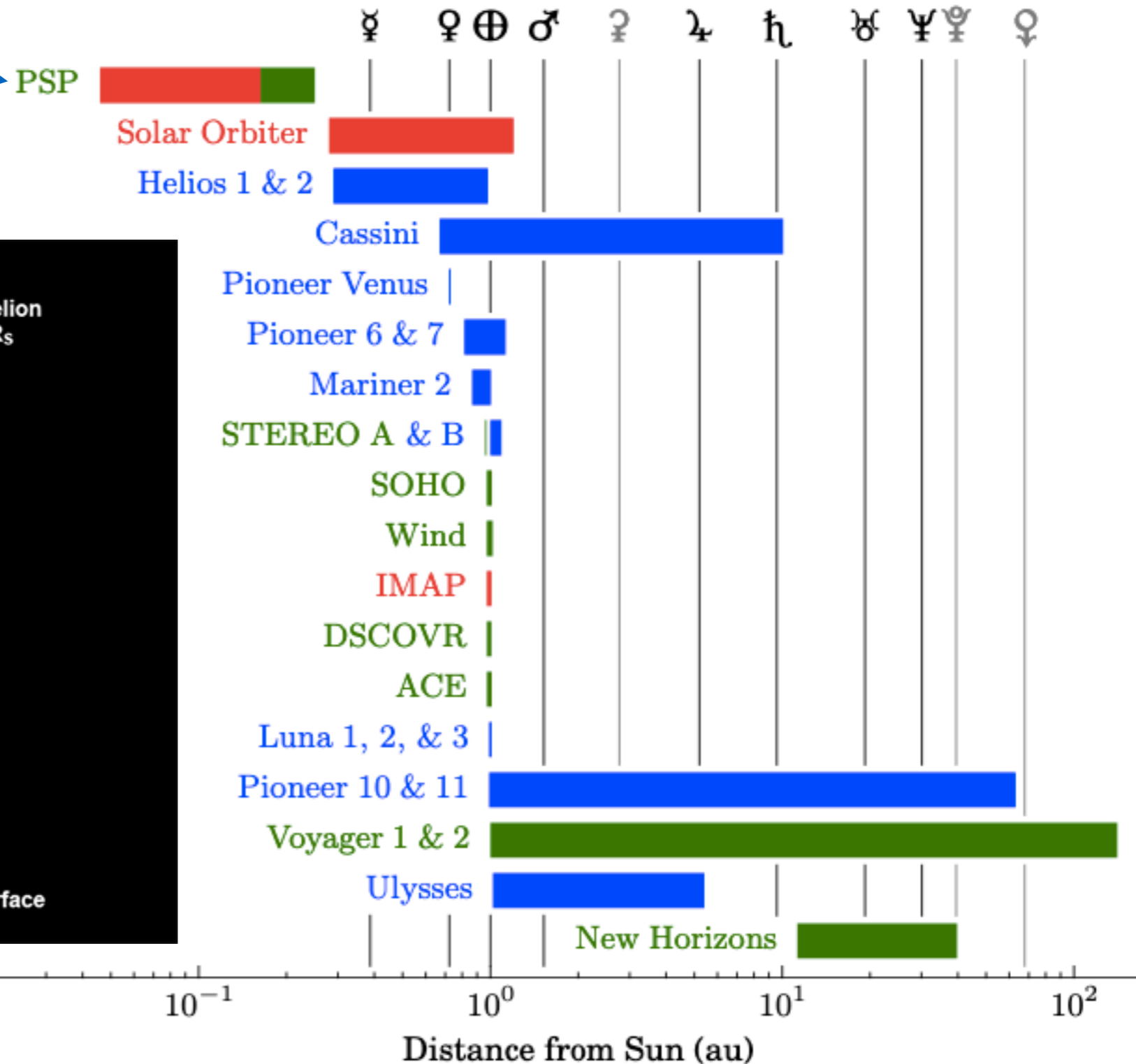
NASA Parker Solar Probe (PSP) mission

Parker Solar Probe: a mission to "touch" the Sun



[credit: NASA]

typically $\beta \ll 1$ regime



[credit: Verscharen, Klein & Maruca (arXiv:1902.03448)]

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The hybrid-PIC code PEGASUS++

[Kunz et al., JCP (2014)]

- **Fully kinetic ions** (Vlasov equation through Lagrangian approach)
- **Massless electron fluid** (generalized Ohm's law)
- **Maxwell's equations** (Faraday equation + Ampere's law w/o displacement current)

$$\frac{\partial f_i}{\partial t} + \mathbf{v} \cdot \nabla f_i + \frac{e}{m_i} \left[\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} + \frac{\mathbf{F}_{\text{ext}}}{m_i} \right] \cdot \frac{\partial f_i}{\partial \mathbf{v}} = 0,$$

$$\mathbf{E} = -\frac{\mathbf{u}_i}{c} \times \mathbf{B} + \frac{(\nabla \times \mathbf{B}) \times \mathbf{B}}{en_i c} - \frac{T_{e,0} \nabla n_i}{en_i},$$

$$\frac{\partial \mathbf{B}}{\partial t} = -c \nabla \times \mathbf{E},$$

- Quasi-neutrality is assumed ($n_e = n_i$)
- Time-correlated external forcing injecting momentum fluctuations at a prescribed power input rate
- An isothermal closure for electrons' pressure is adopted
- Small-scale dissipation: hyper-resistivity + numerical filters (only on the first two moments of f_i , i.e., n_i and $n_i \mathbf{u}_i$)

Simulation setup

$$\beta_{i,0} = 1/9 \simeq 0.11$$

$$T_{e,0}/T_{i,0} = 1$$

$$L_{\parallel} = 6L_{\perp} = 48\pi d_i \simeq 151d_i (\simeq 452\rho_i)$$

$$N_x = N_y = 288$$

$$N_z = 1728$$

$$\Delta \simeq 0.087d_i (\simeq 0.26\rho_i)$$

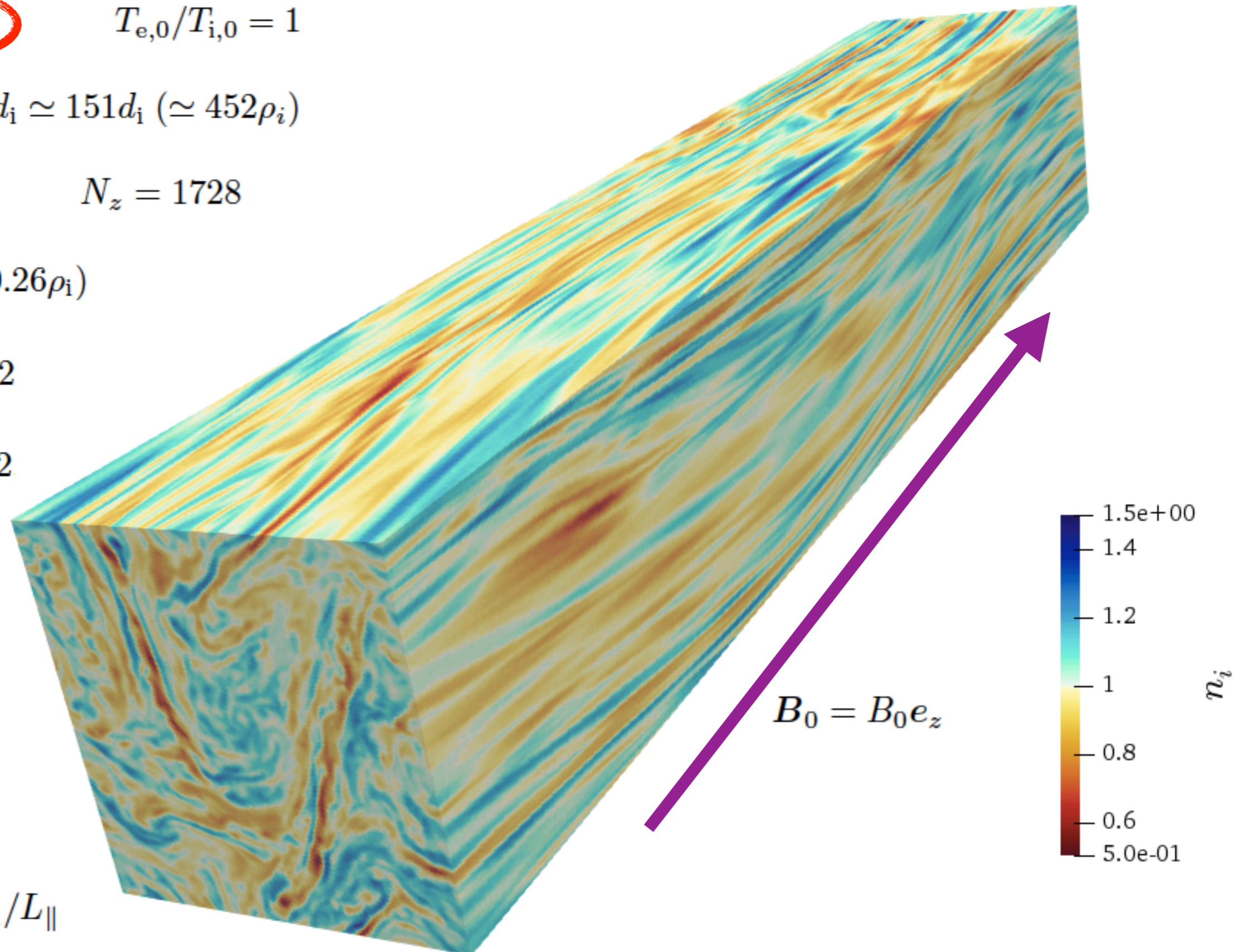
$$0.083 \lesssim k_{\perp}\rho_i \lesssim 12$$

$$0.014 \lesssim k_{\parallel}\rho_i \lesssim 12$$

512 ppc

$$\nabla \cdot F = 0$$

$$\delta u_{\perp}^{(\text{rms})}/v_A \approx L_{\perp}/L_{\parallel}$$

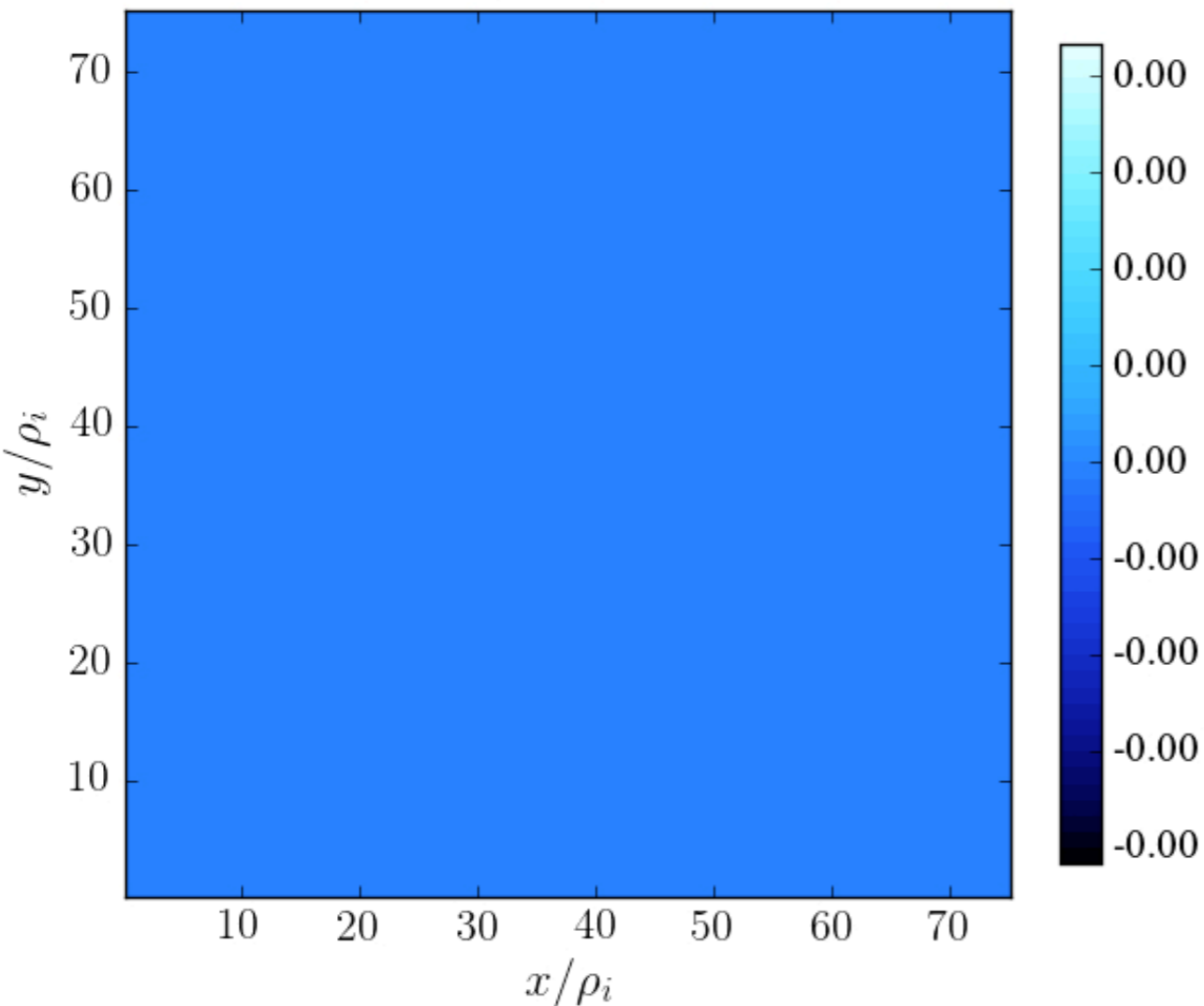


Outline

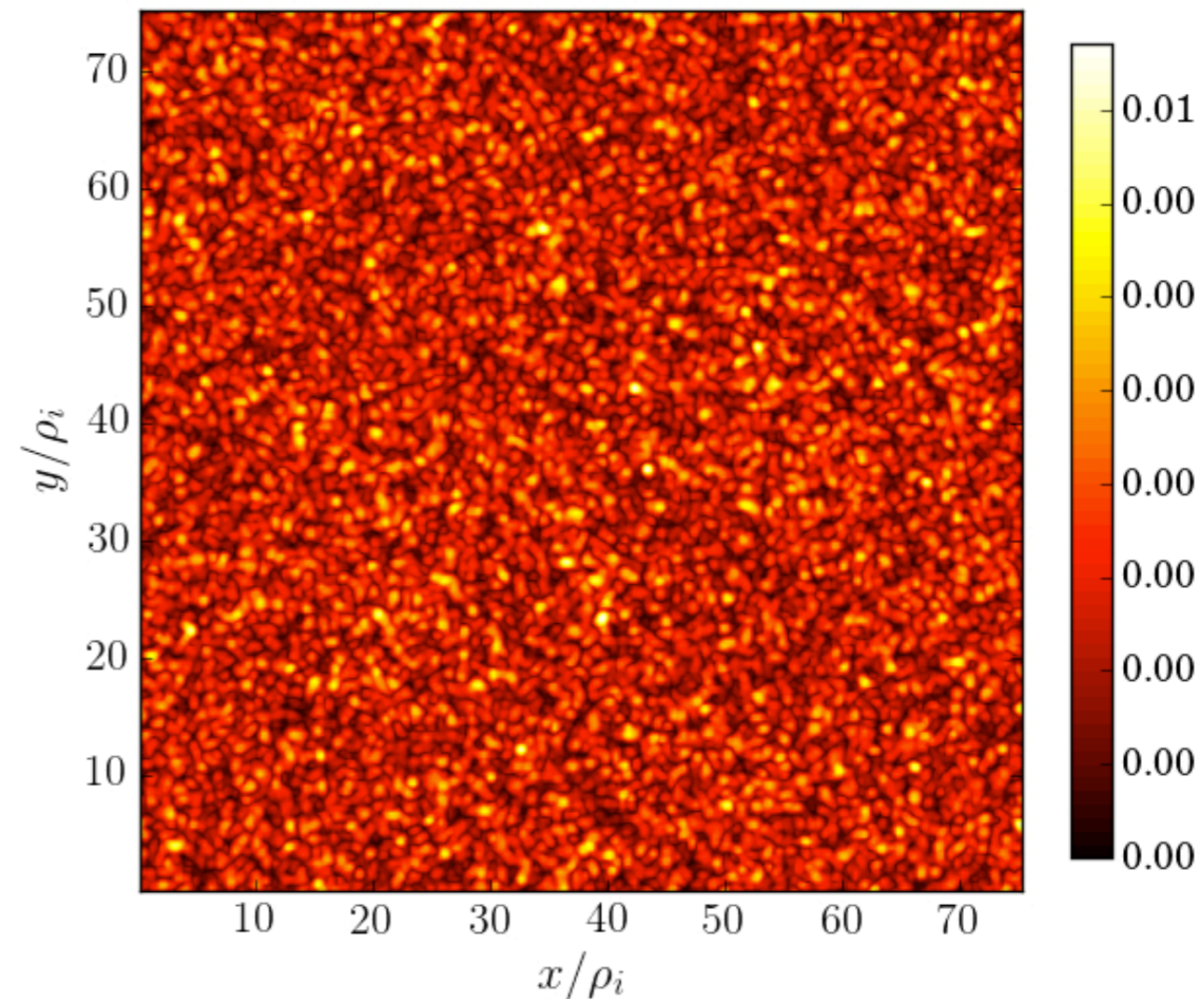
- Turbulence & heating in astrophysical and space plasmas
 - ☞ Why do we care about turbulence in “collisionless” plasmas?
 - ☞ The solar wind & space missions (*or, “where we can really learn something about plasma turbulence”*)
 - ☞ What (we think) we know about plasma turbulence and turbulent heating
 - ☞ The NASA Parker Solar Probe mission
- The hybrid-PIC code `PEGASUS` & simulation setup
- Magnetic reconnection & spectral features of quasi-steady state turbulence
- Ion heating

An impression of reconnection

δB_{\perp} at $z = 0$

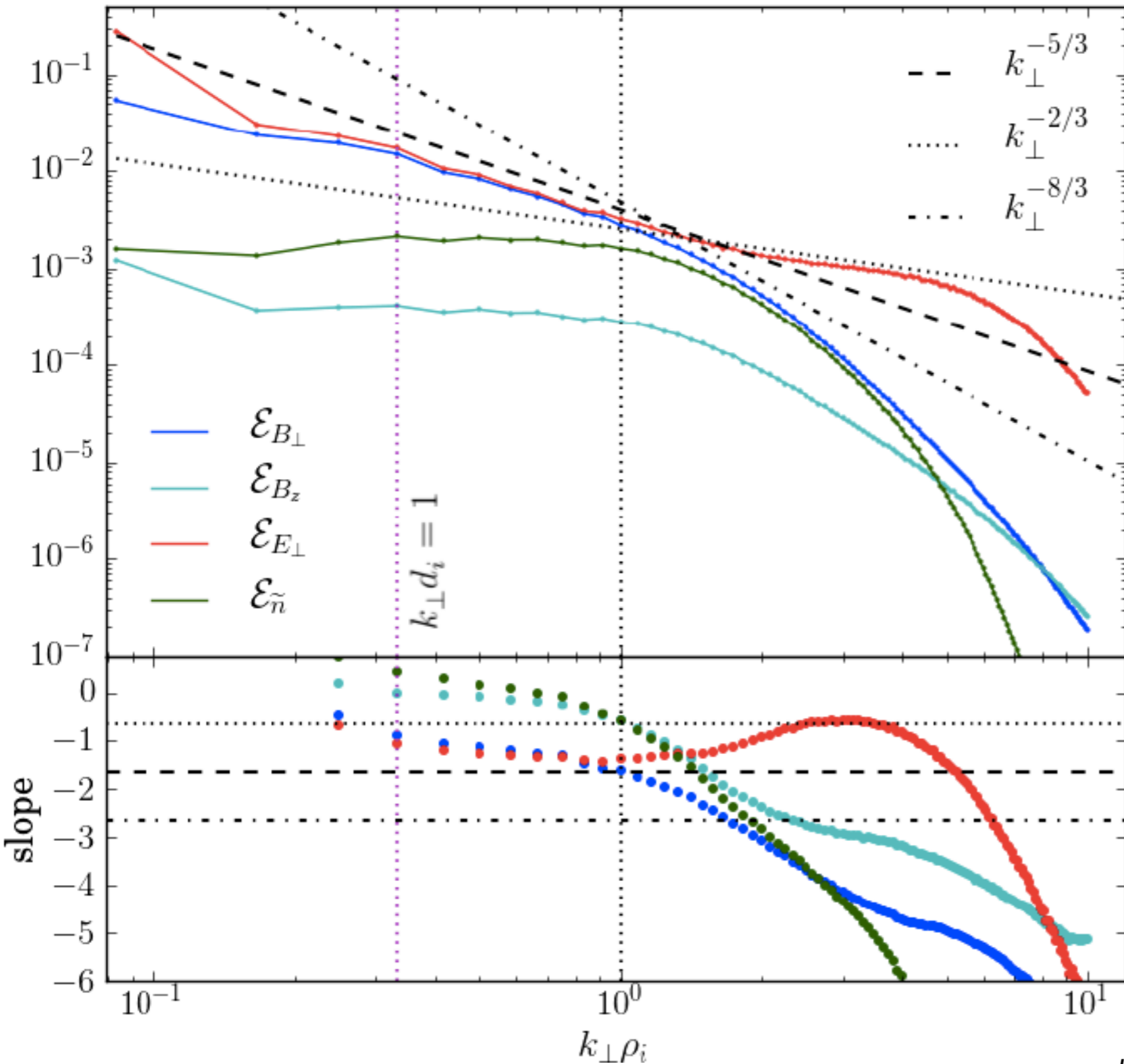


δE_{\perp} at $z = 0$



- First current sheets and reconnection events clearly recognisable
- Several relevant features in spectra and ion heating emerge only after these first events
- Continuous formation and disruption of current sheets via reconnection in quasi-steady turbulent phase

Spectrum of turbulent fluctuations



- Spectral break between d_i and ρ_i
- Polarisation of sub-ion scale fluctuations roughly consistent with KAW-like turbulence (not shown)
- Spectral slopes steeper than the ones predicted by standard KAW turbulence
- Sub-ion-scale spectrum consistent with the picture of “**reconnection-mediated**” kinetic turbulence

see, e.g., for
kinetic case:

Cerri & Califano, NJP (2017)
Franci, Cerri et al., ApJL (2017)

+ “fluid” case:

*Loureiro & Boldyrev, ApJ (2017); Mallet et al., JPP (2017),
Comisso et al., ApJ (2018); Dong et al., PRL (2018),...*

[Cerri, Arzamasskiy & Kunz (in preparation)]

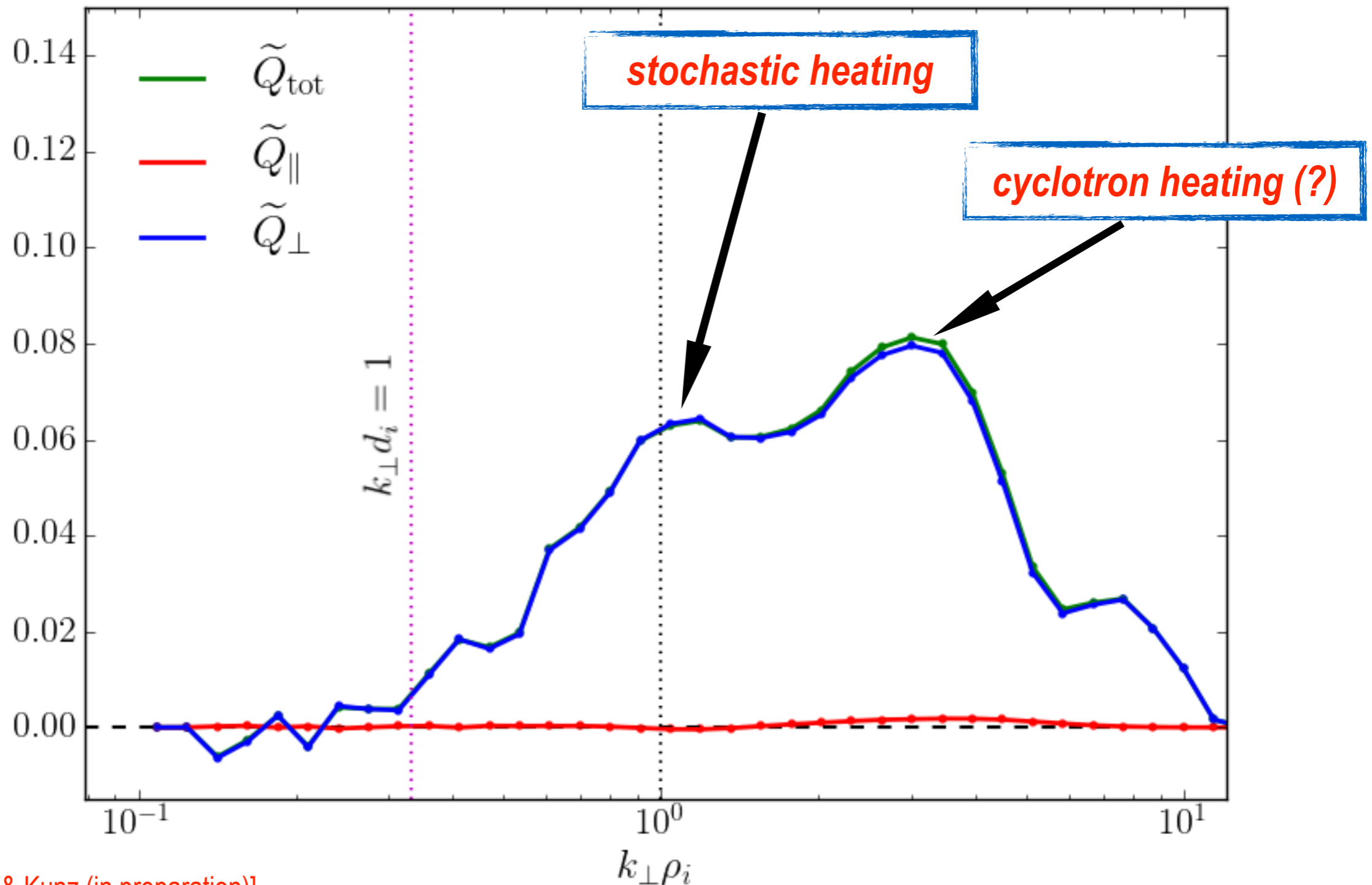
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Ion heating in k-space

Ion heating averaged over the quasi-steady turbulent phase

$$\tilde{Q}_{\parallel,\perp} = \frac{1}{Q_{\text{tot}}} \sum_{\text{particles}} w_{\parallel,\perp} \cdot E_{\parallel,\perp}(k_{\perp})$$

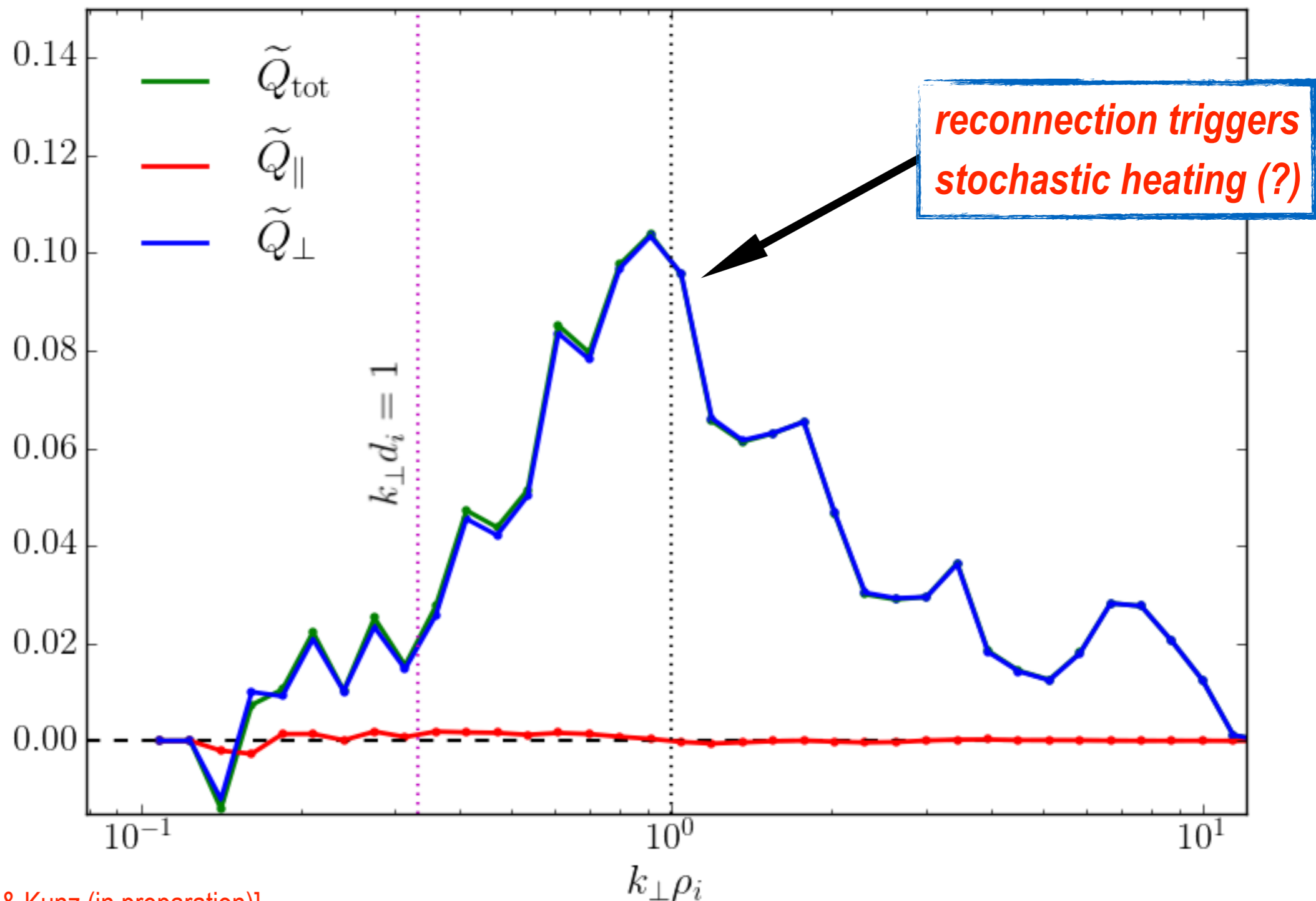


[Cerri, Arzamasskiy & Kunz (in preparation)]

Ion heating in k-space

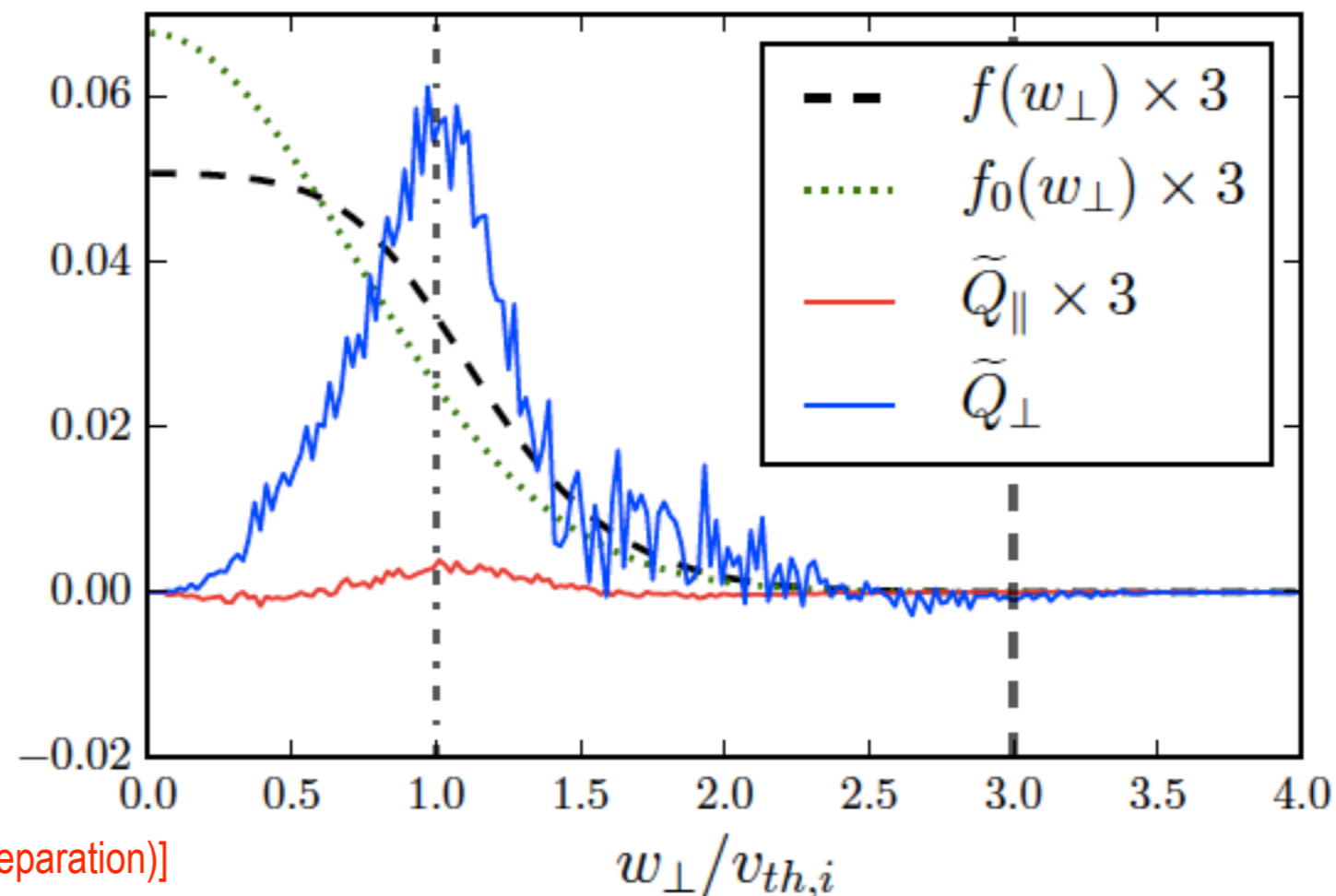
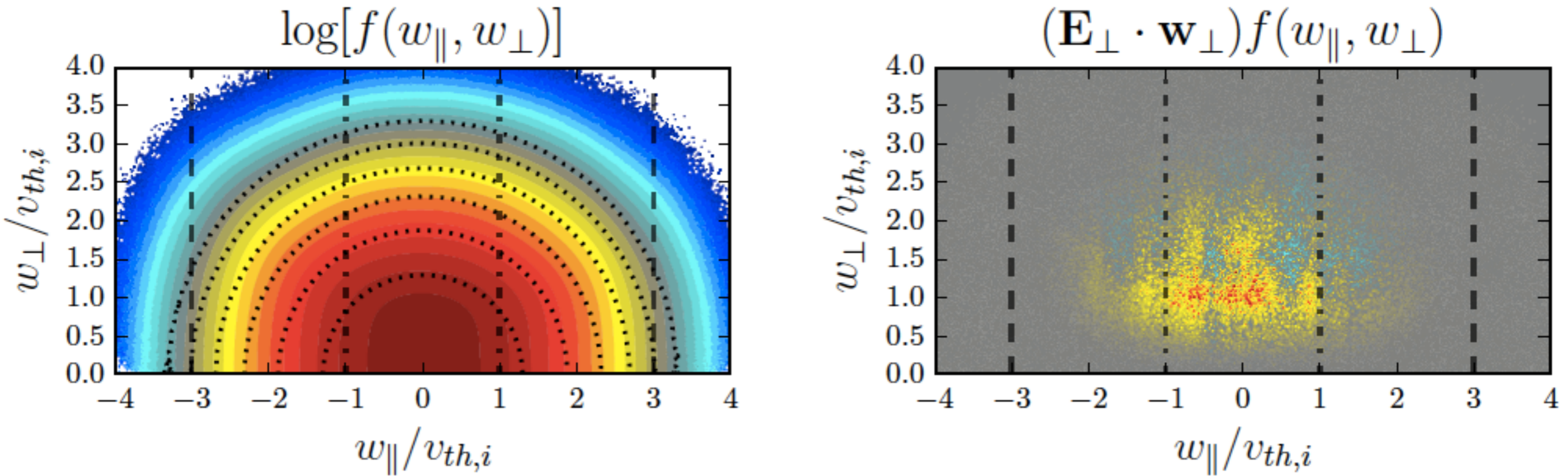
Ion heating averaged over the onset of the first reconnection events

$$\tilde{Q}_{\parallel,\perp} = \frac{1}{Q_{\text{tot}}} \sum_{\text{particles}} w_{\parallel,\perp} \cdot E_{\parallel,\perp}(k_{\perp})$$



[Cerri, Arzamasskiy & Kunz (in preparation)]

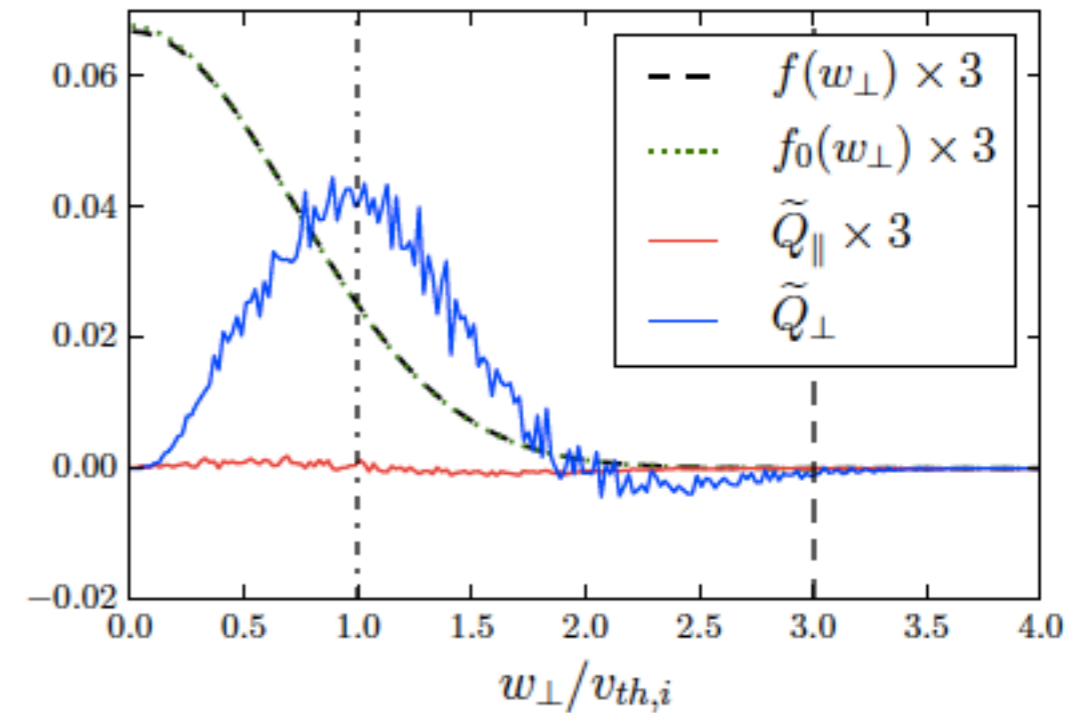
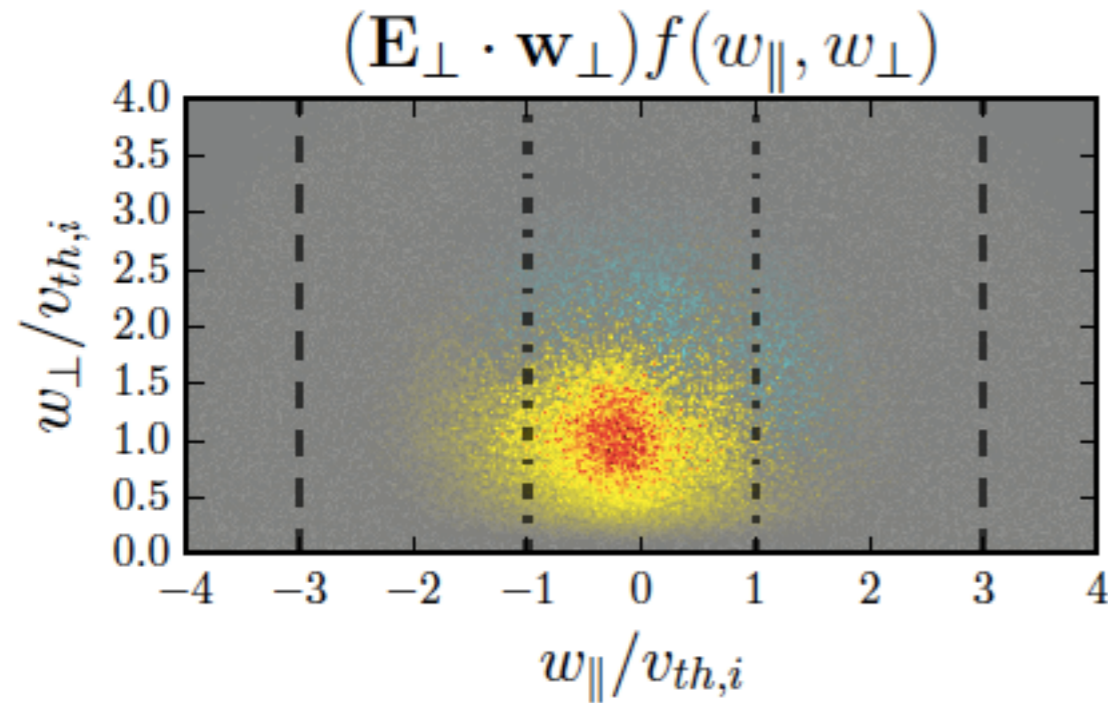
Ion heating in velocity space



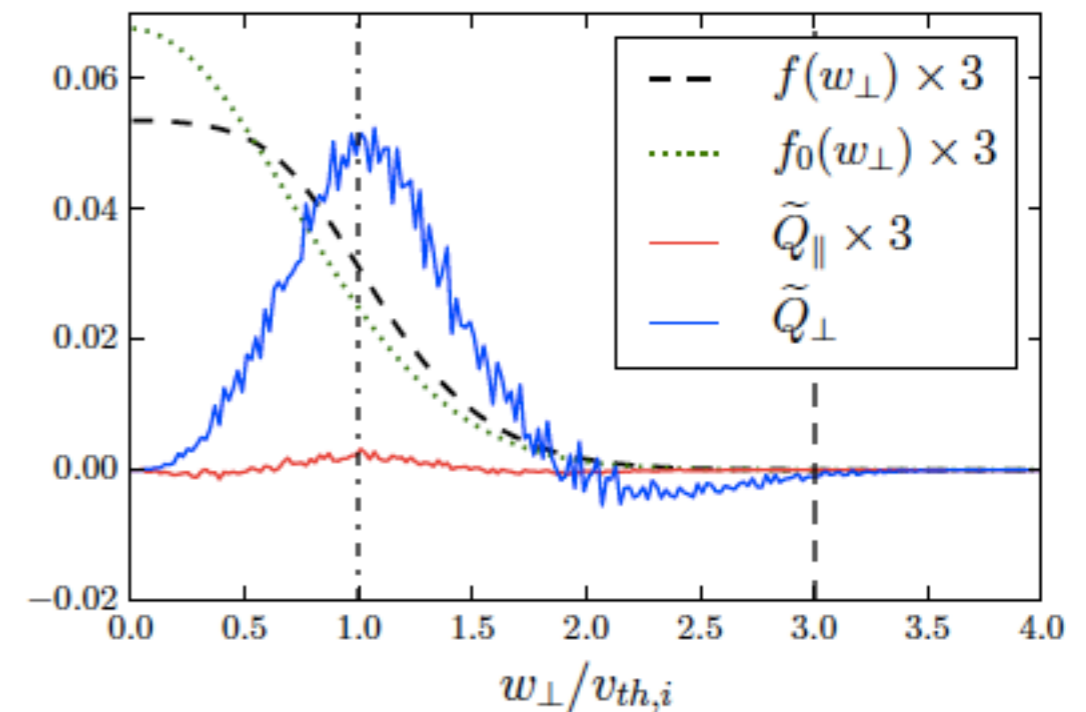
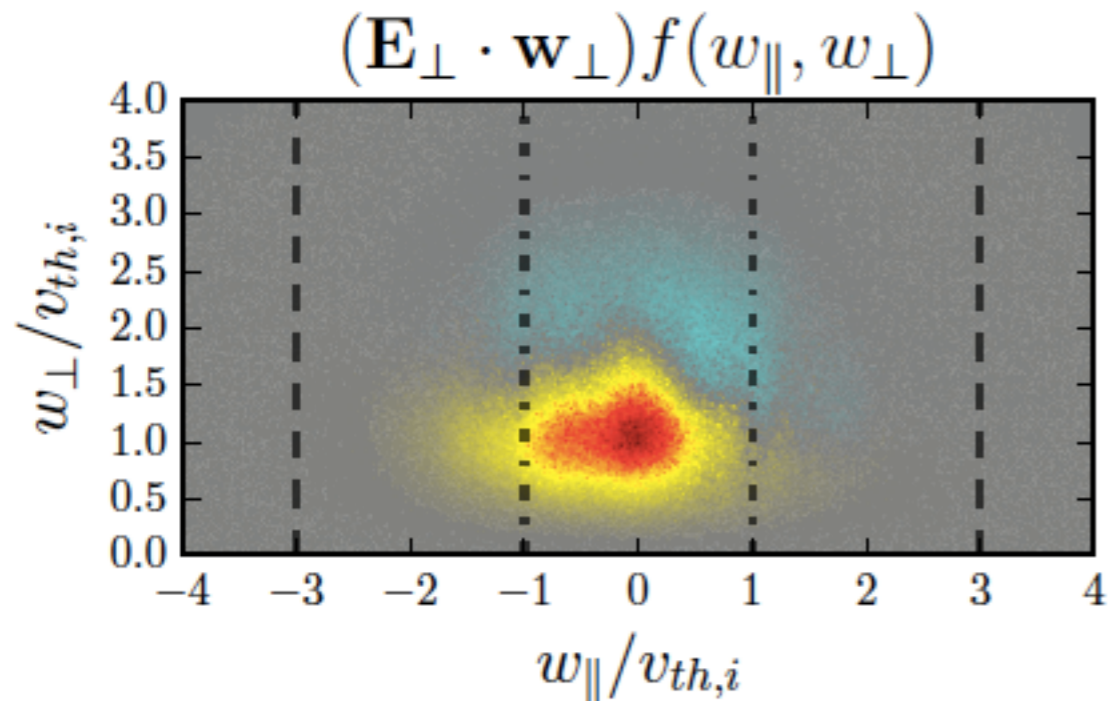
[Cerri, Arzamasskiy & Kunz (in preparation)]

Ion heating in velocity space

☞ averaged over the **onset of the first reconnection events**:



☞ averaged over the **entire quasi-steady turbulent phase**:



[Cerri, Arzamasskiy & Kunz (in preparation)]

Conclusions

- ▶ *In low- β (hybrid-kinetic) turbulence, ion heating is predominantly perpendicular to B ($Q_{\parallel} / Q_{\text{tot}} \sim 1.5\%$)*
 - ▶ *Magnetic reconnection seems to play a relevant role in determining the transition to quasi-steady state turbulence and in “activating” (some of the) ion-heating mechanisms*
 - ▶ *Simultaneous presence of stochastic ion heating and (possibly) ion-cyclotron heating (to be further investigated — very intermittent behaviour in time!)*
 - ▶ *From this simulation we estimate that only ~40% of the injected power goes into ion heating (still about an order of magnitude larger than GK prediction)*
- ☞ *This regime is particularly relevant for **Parker Solar Probe**, so... let's see!*

Thank you!